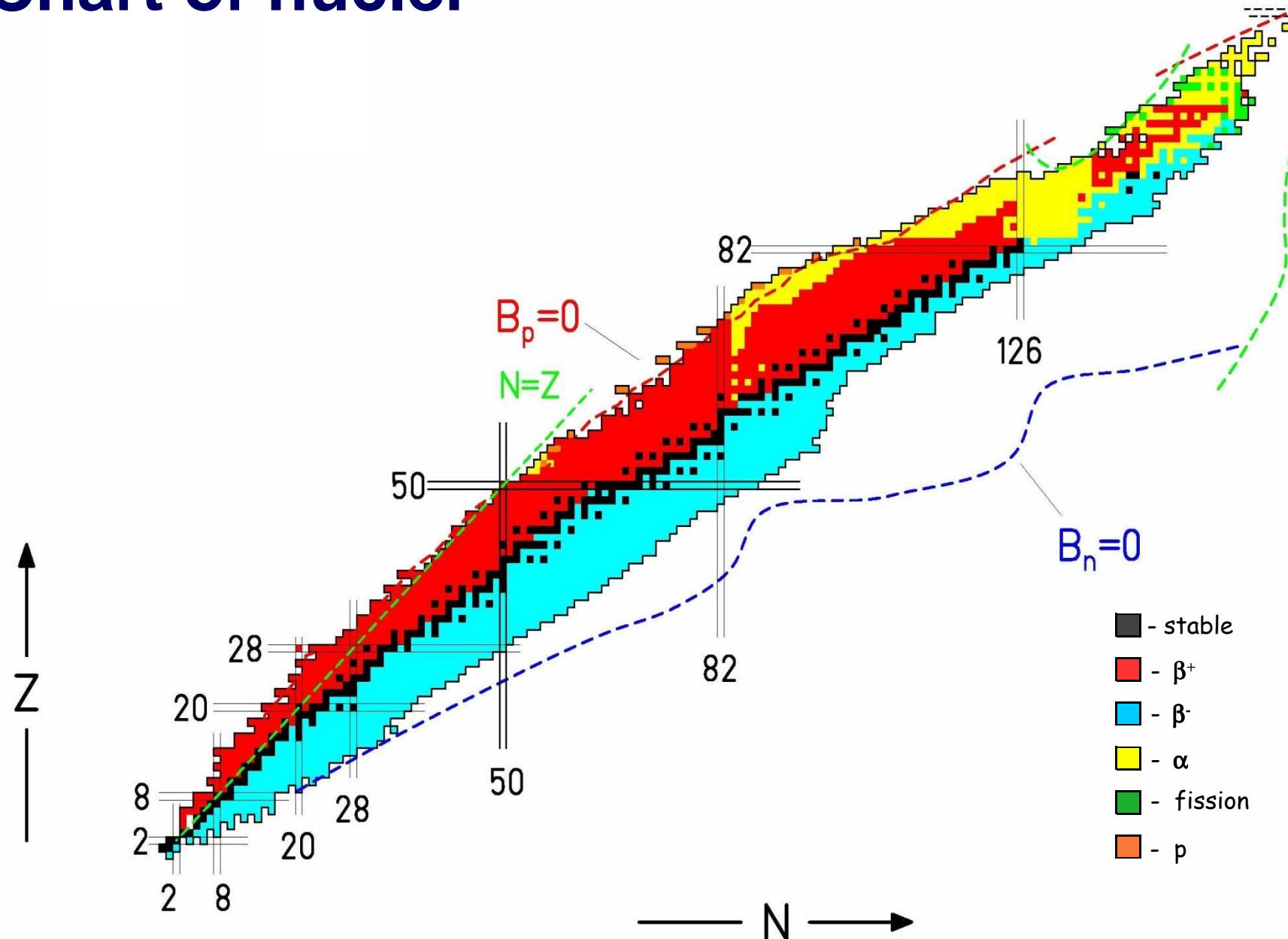


# **Radioactivity at the limits of nuclear existence**

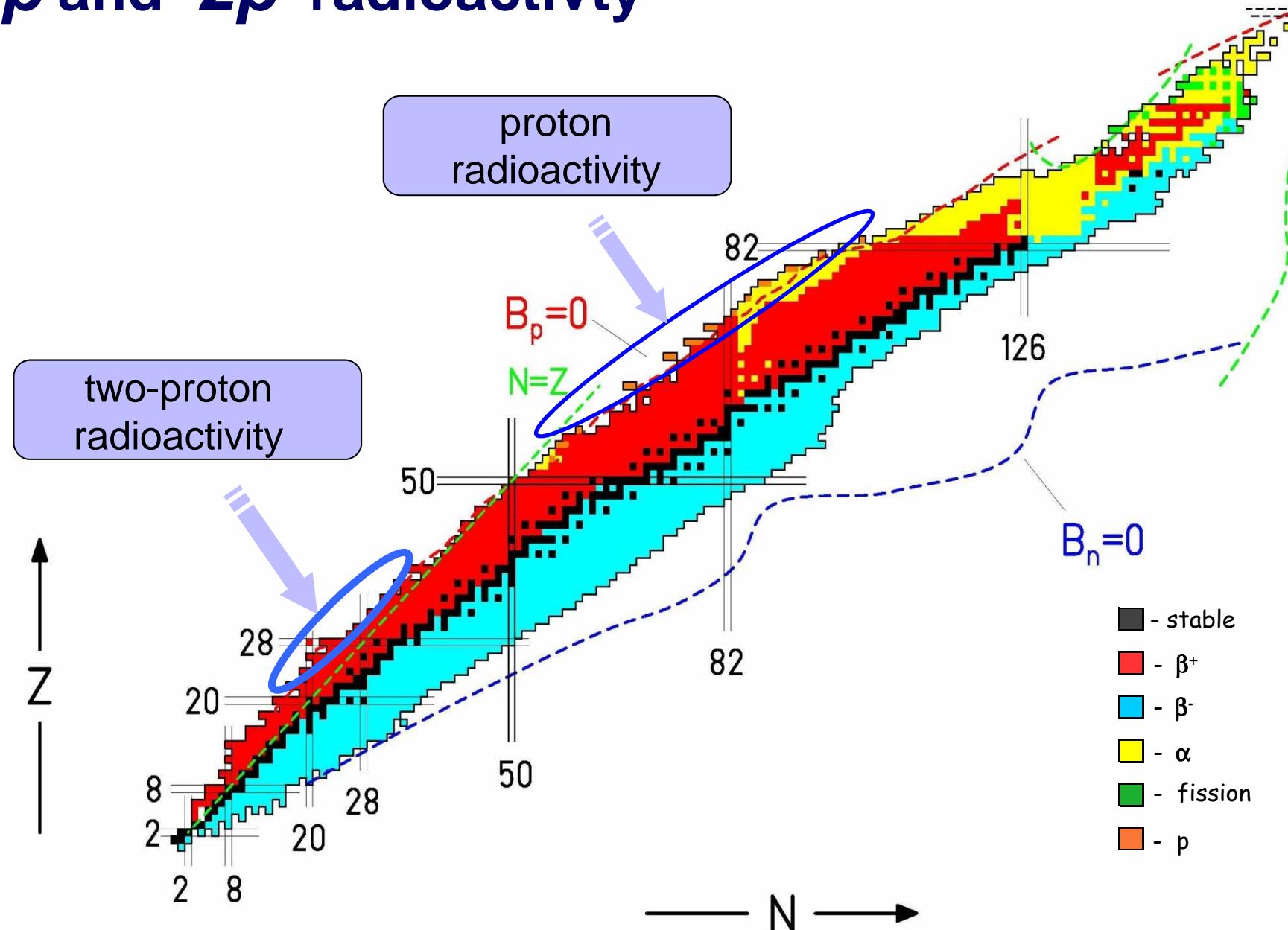
Zenon Janas

Institute of Experimental Physics  
University of Warsaw

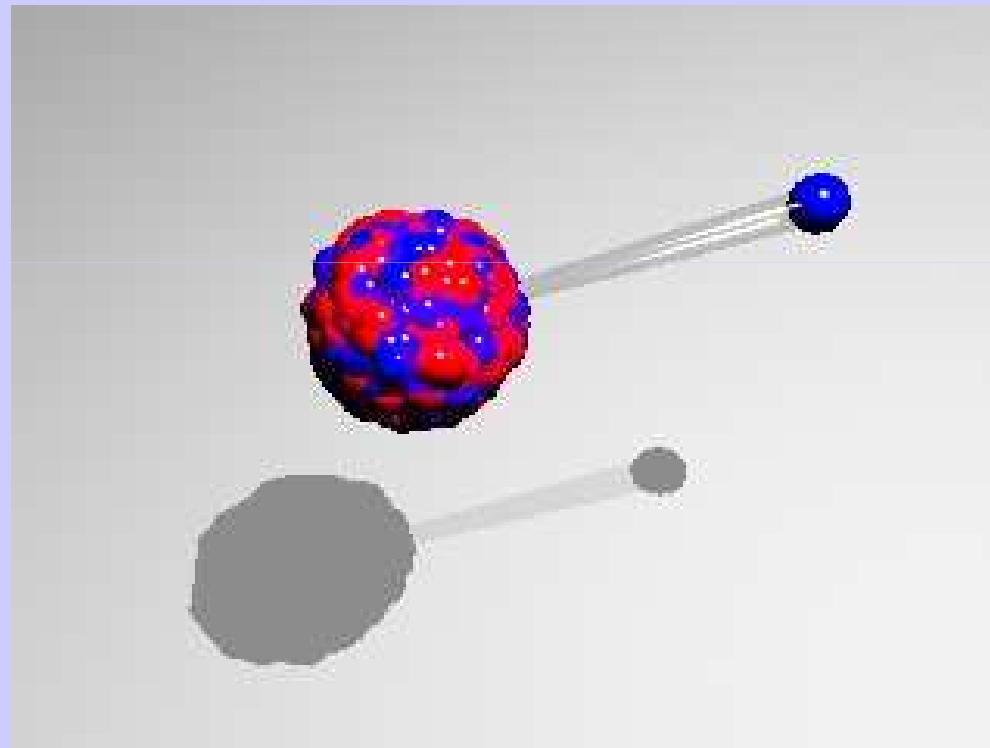
# Chart of nuclei



# *p* and *2p* radioactivity

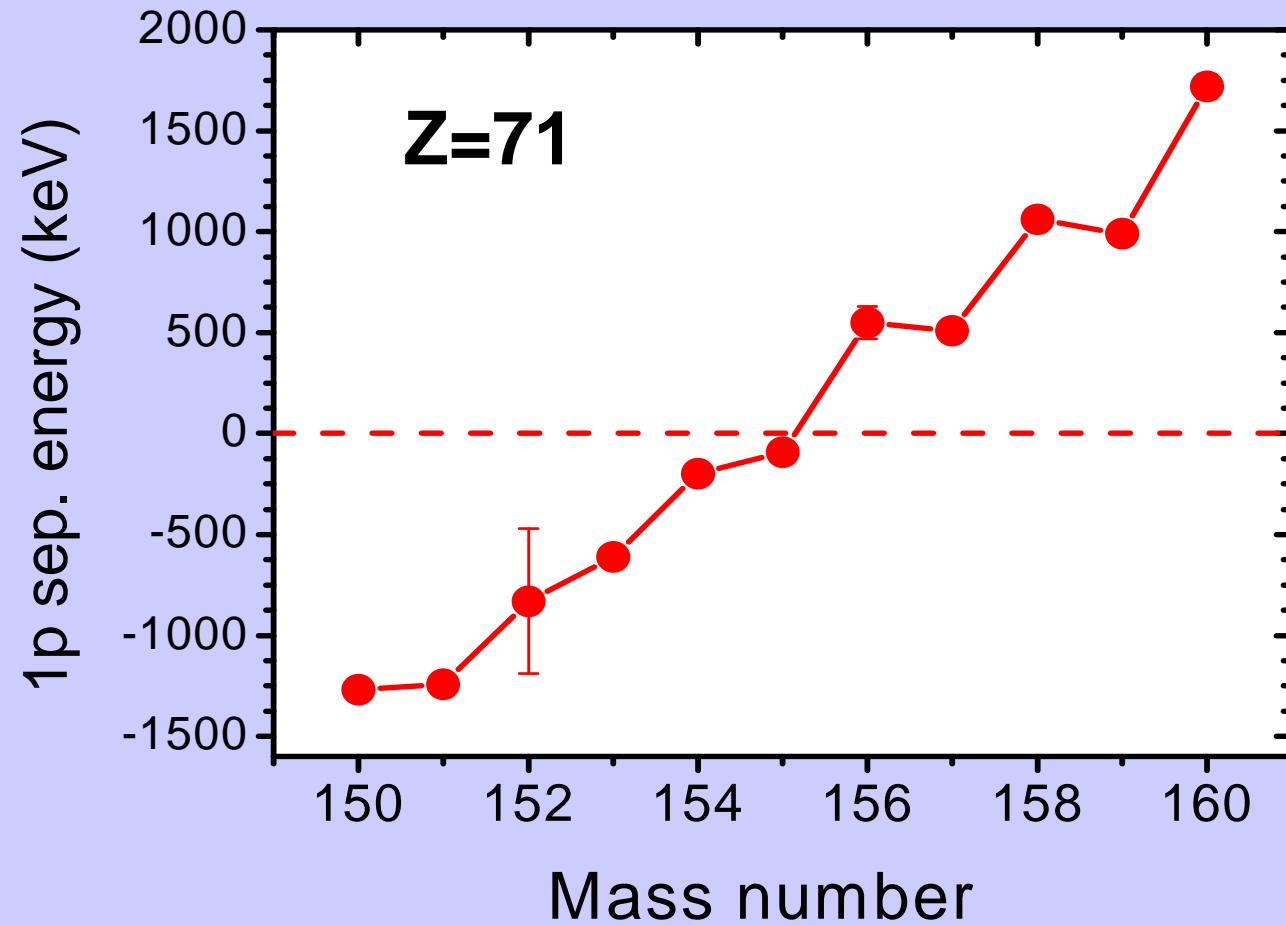


# Proton radioactivity



# History of studies of proton radioactivity

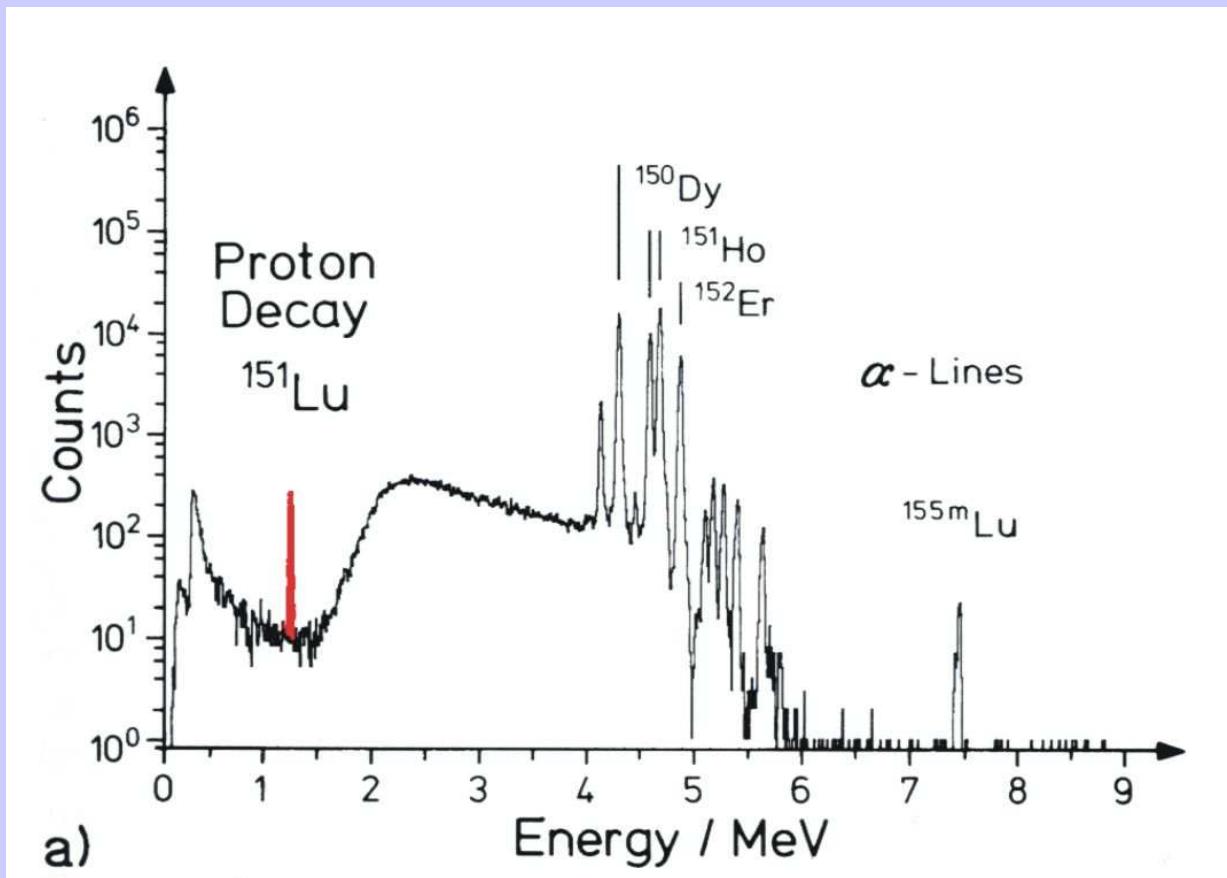
- 1960 – prediction of possibility of  $p$  emission



$^{175}\text{Lu}$   
stable

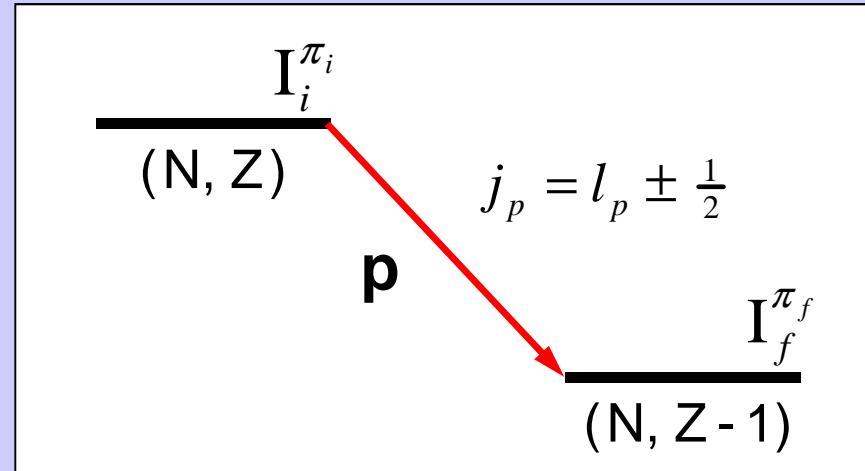
# History of studies of proton radioactivity

- 1981 – observation of  $^{151}\text{Lu} \rightarrow ^{150}\text{Yb} + \text{p}$  decay



$$\begin{aligned}E_p &= 1233 \text{ keV} \\T_{1/2} &= 85 \text{ ms} \\b_p &= 70\%\end{aligned}$$

# Proton radioactivity



Energy conservation

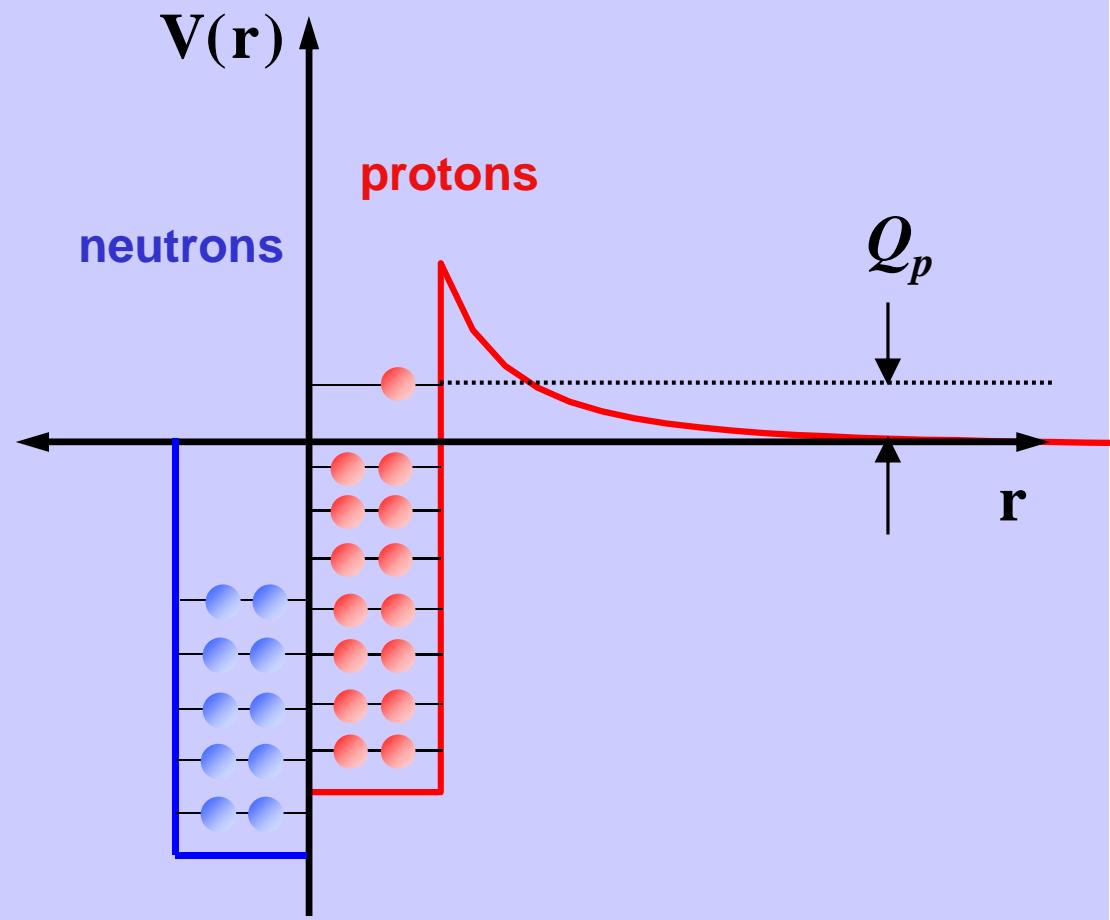
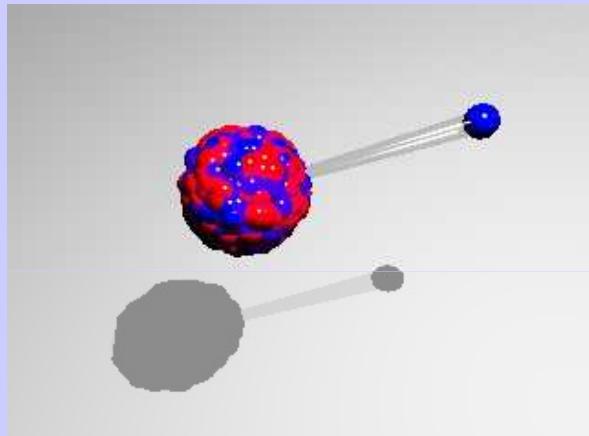
$$Q_p = M_i c^2 - M_f c^2 - m_H c^2 = -S_p > 0$$

Angular momentum and parity conservation

$$\vec{I}_i = \vec{I}_f + \vec{l}_p + \frac{1}{2}$$

$$\pi_i \cdot \pi_f = (-1)^{l_p}$$

# Proton radioactivity



# Probability of proton emission

$$\lambda_p = S \cdot \nu \cdot P_{lj}$$

$S$  – spectroscopic factor

$\nu$  – frequency of proton movement in nucleus

$$\nu = \frac{v}{2R} \approx 6 \cdot 10^{21} \text{ s}^{-1}$$

$P_{lj}$  – probability of barrier penetration

$$P_{lj} = e^{-2G_{lj}}$$

$G_{lj}$  – Gamow's factor

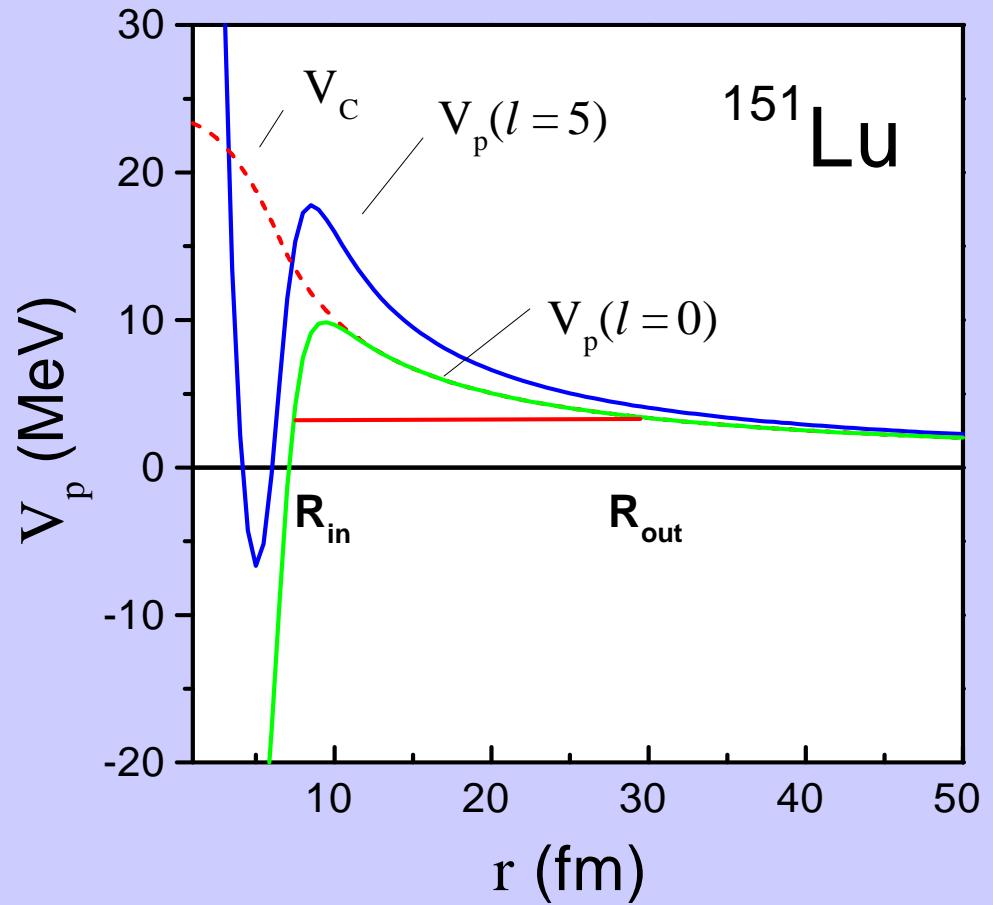
# Gamow's factor

$$G_{\ell j} = \int_{R_{in}}^{R_{out}} \sqrt{\frac{2\mu}{\hbar^2} \left( V_p(r) - \tilde{Q}_p \right)} dr$$

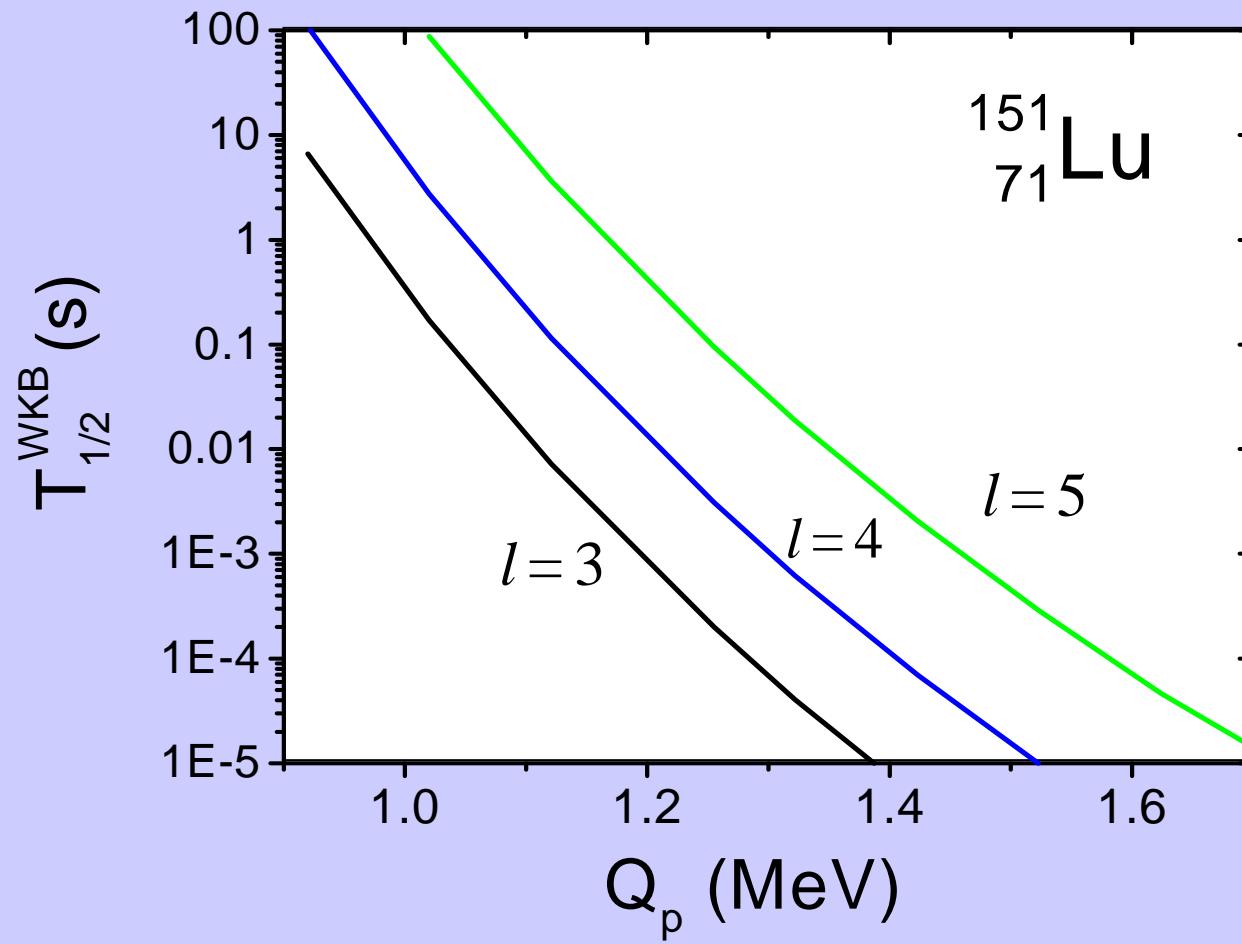
$V_p(r)$  – interaction potential

$$V_p(r) = V_N(r) + V_C(r) + V_l(r)$$

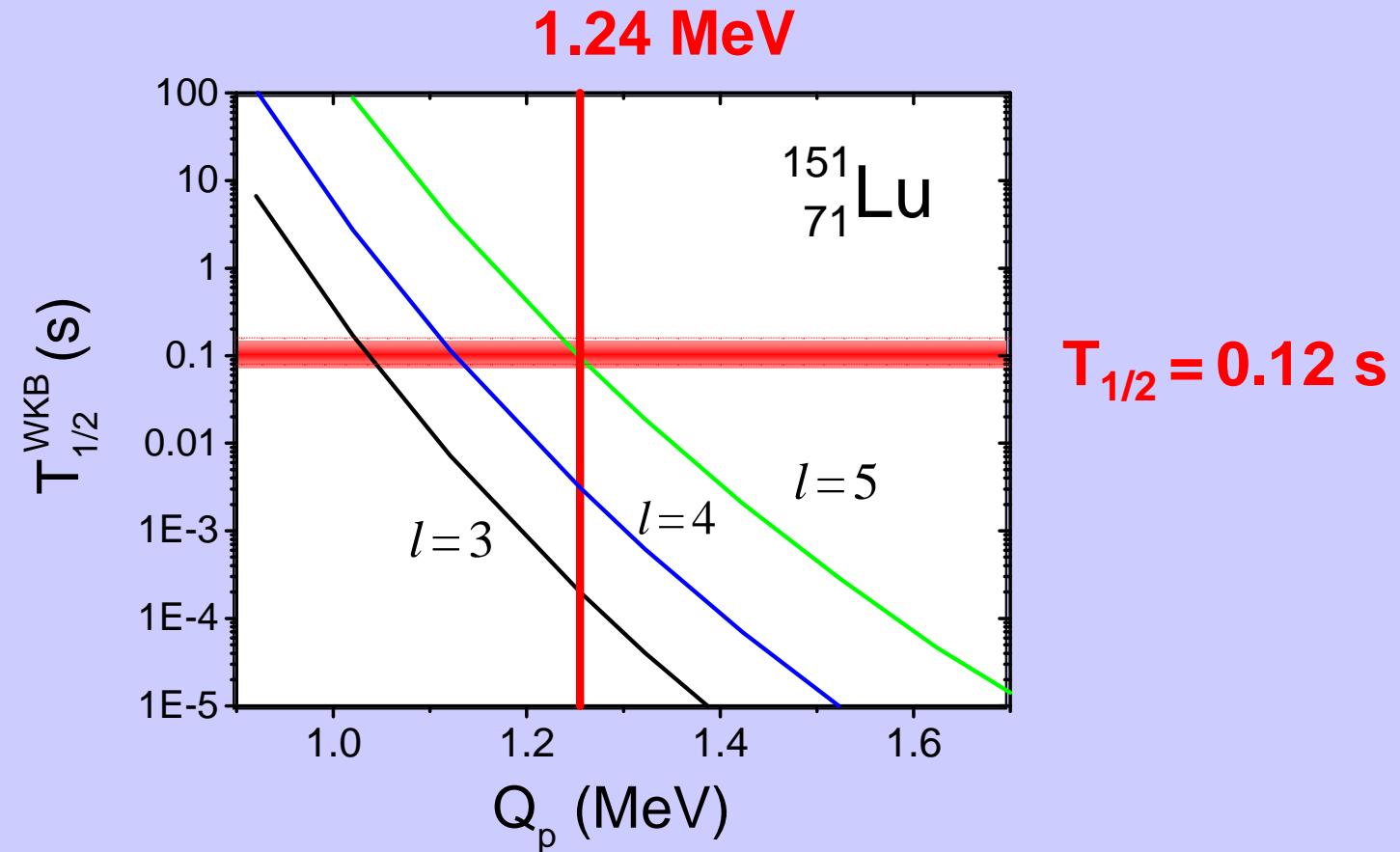
$R_{in}, R_{out}$  – turning points



# WKB calculations for $^{151}\text{Lu}$



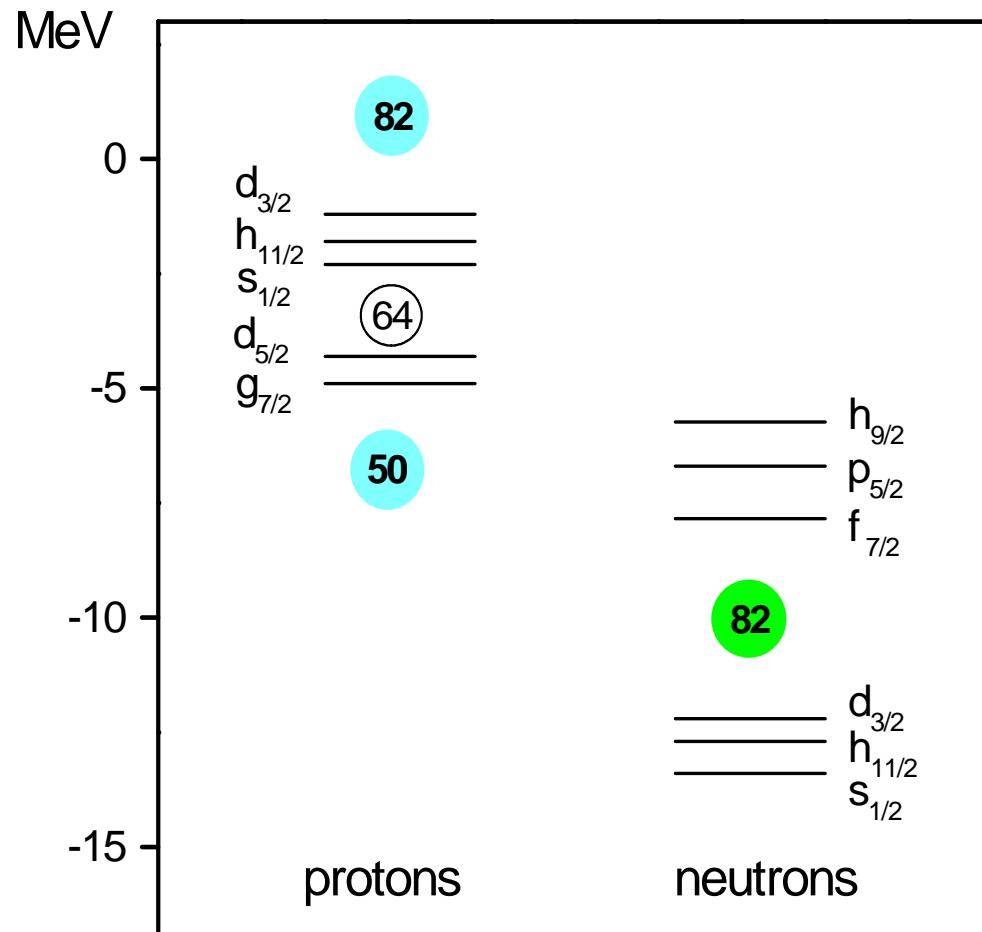
# WKB calculations for $^{151}\text{Lu}$



for  $l_p = 5$

$$\frac{T_{1/2}^{\text{WKB}}}{T_{1/2}^{\text{exp}}} = 0.6$$

# Single-particle states



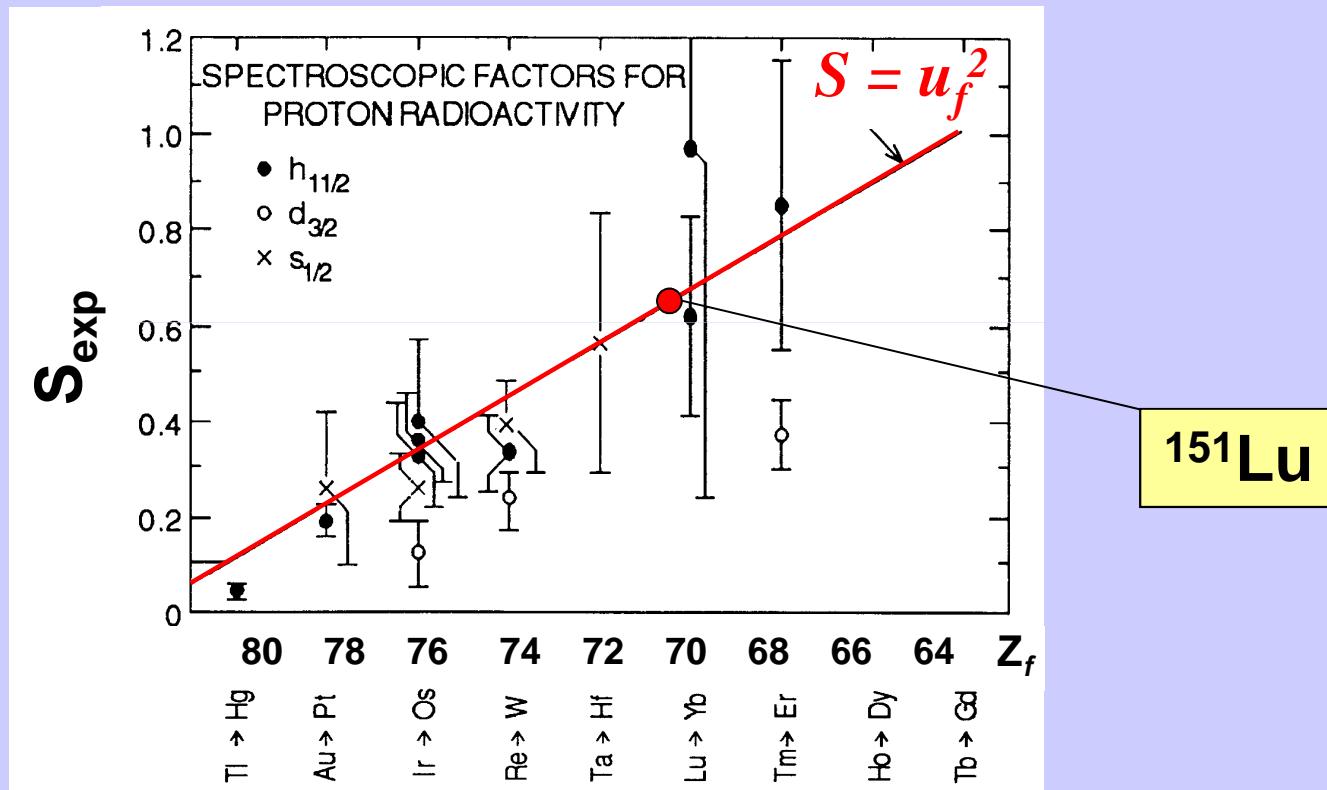
Valent particles:

5 protons on  $h_{11/2}$

2 neutrons on  $d_{3/2}$

# $S$ factors for $p$ emitters with $64 < Z < 82$

- filled proton orbitals :  $s_{1/2}$ ,  $d_{3/2}$  i  $h_{11/2}$

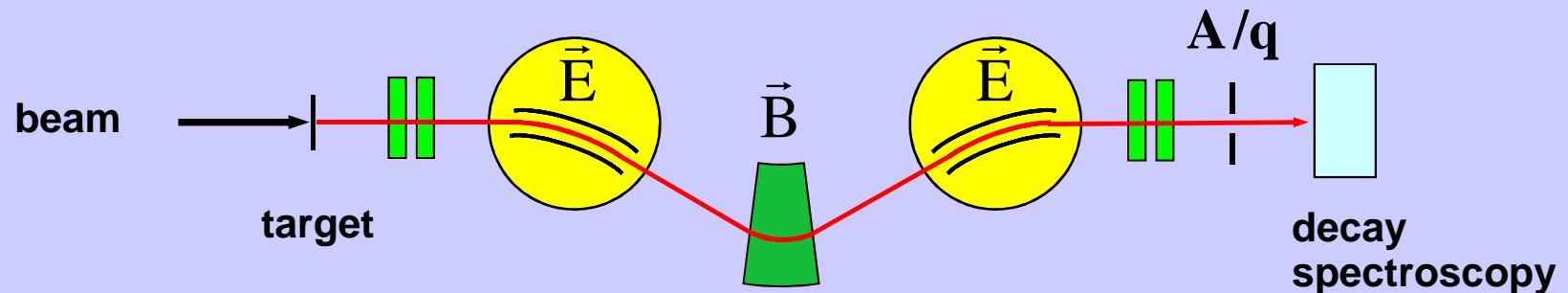


# Proton decay of $^{131}_{63}\text{Eu}$

- production in fusion-evaporation reaction

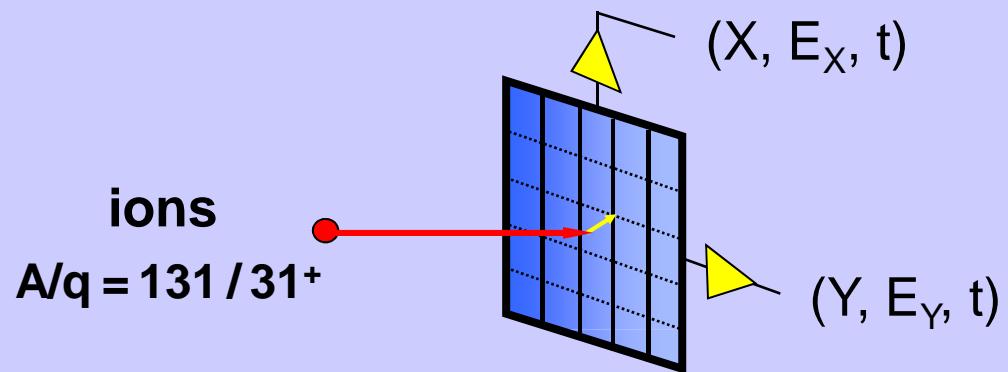


- recoil mass separation (FMA – Argonne)



- decay spectroscopy

**detector** Double-sided **S**ilicon **S**trip **D**etector



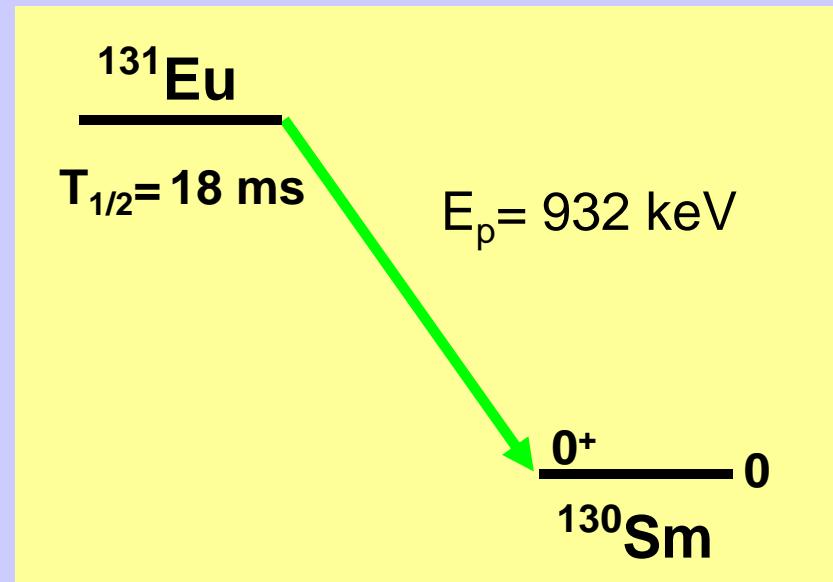
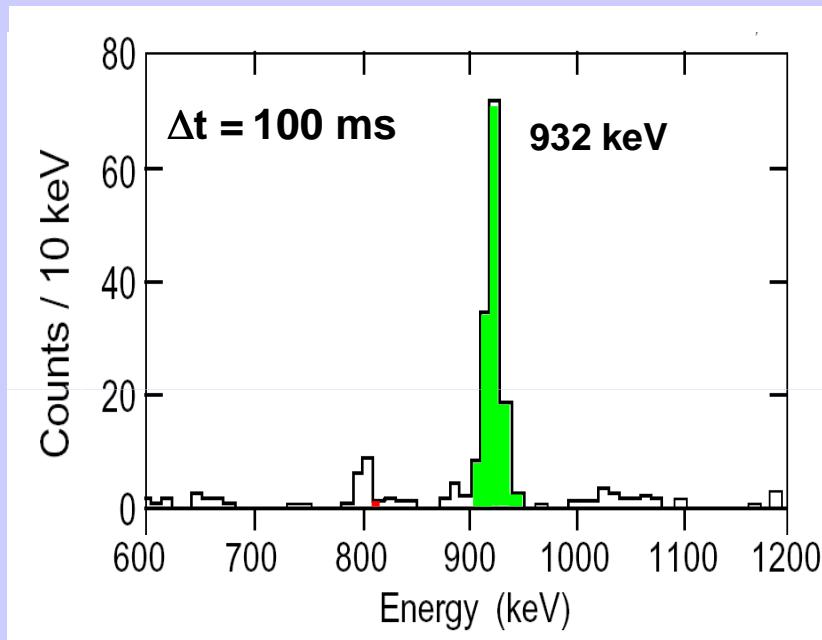
Typical parameters:

**40 × 40 × 0.1 mm**  
**40 × 40 strips**

Registration of (X, E<sub>x</sub>, t) and (Y, E<sub>Y</sub>, t) enables:

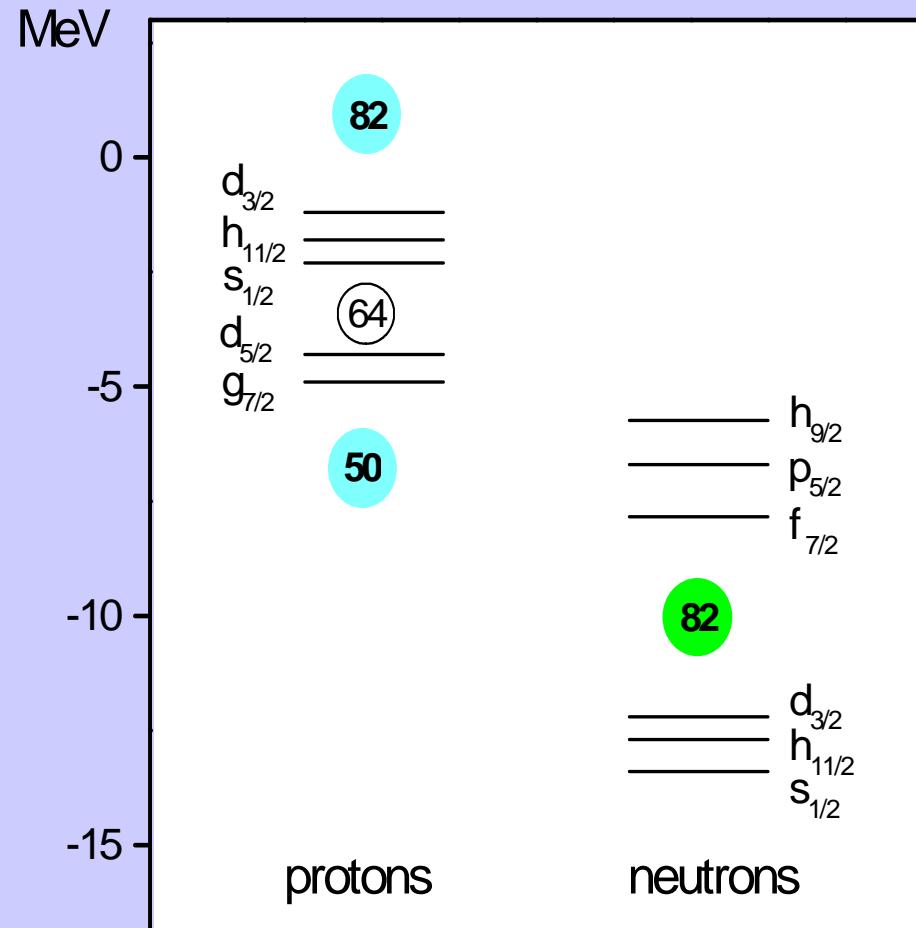
- determination of X and Y position
- energy measurement
- determination of implantation – decay time

# Proton decay of $^{131}_{63}\text{Eu}$

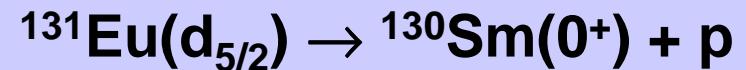


120 hours of measurement

# Single-particle states for $^{131}_{63}\text{Eu}$



for transition



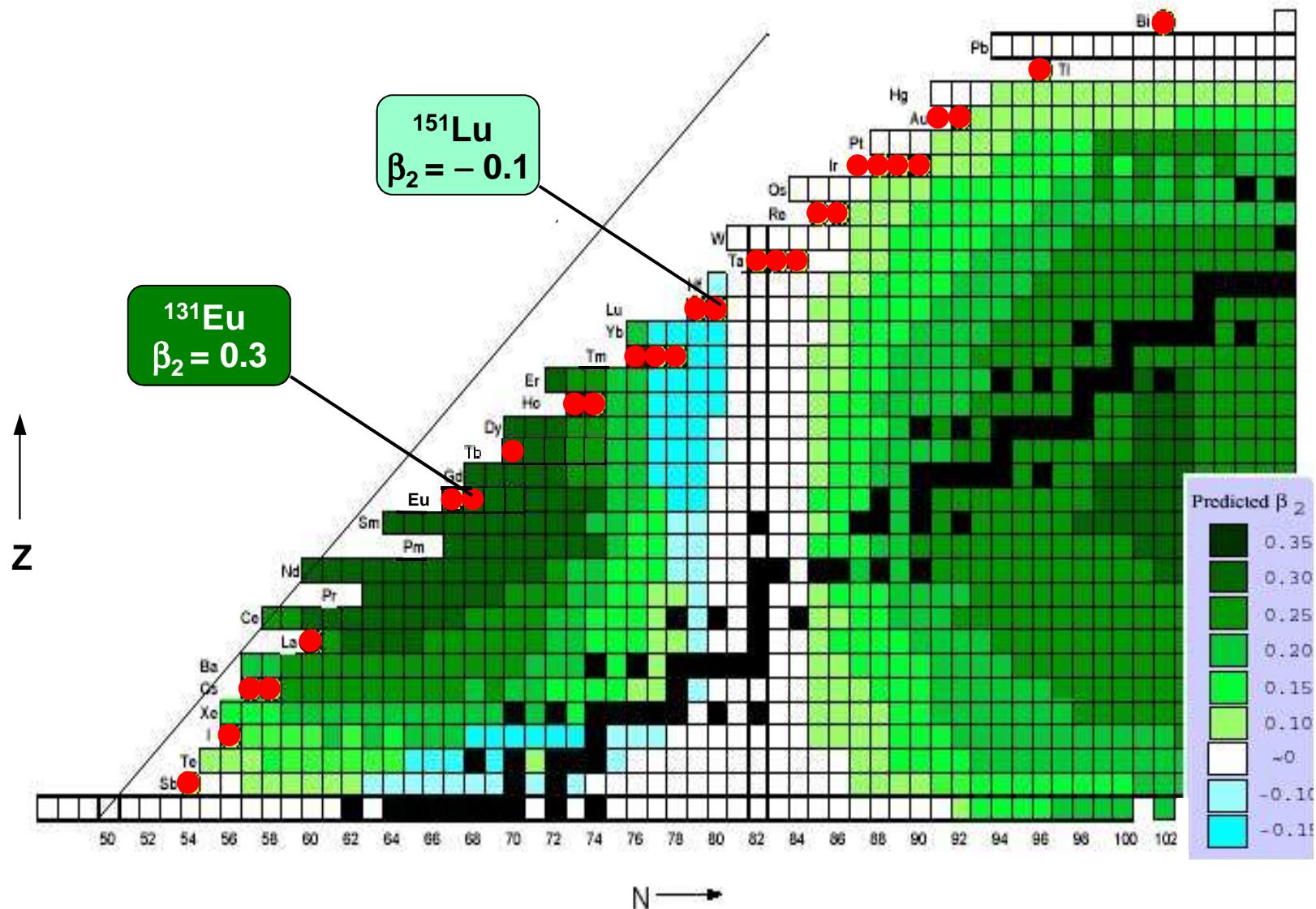
$$l_p = 2 \quad T_{1/2}^{WKB} = 0.5 \text{ ms}$$

$$S_{exp} = \frac{0.5 \text{ ms}}{18 \text{ ms}} = 0.02$$

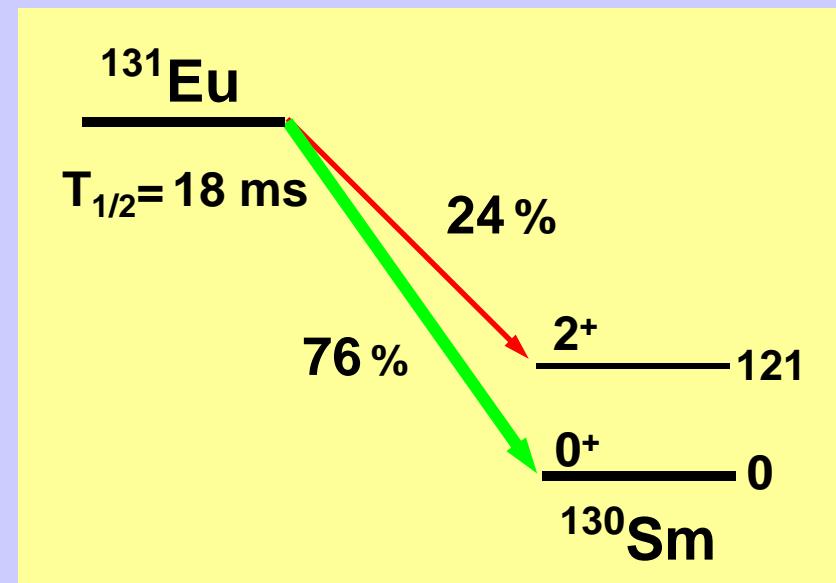
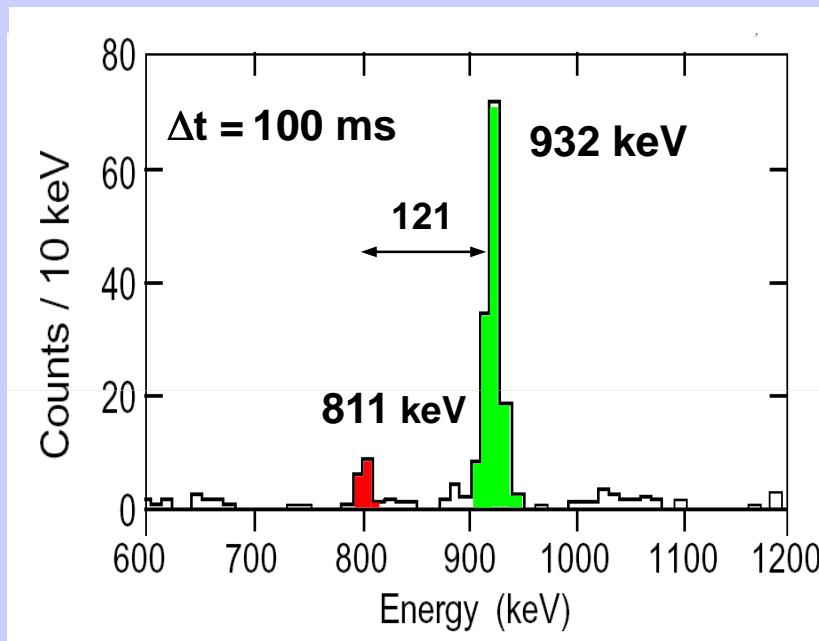
!!!

$$S_{th} = u_j^2 = 0.52$$

# Map of nuclear deformation



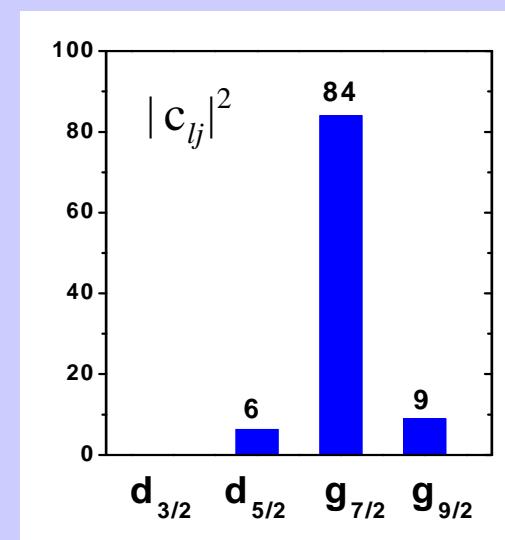
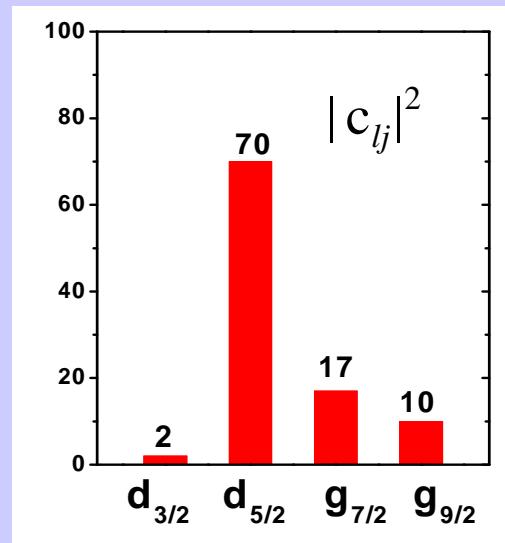
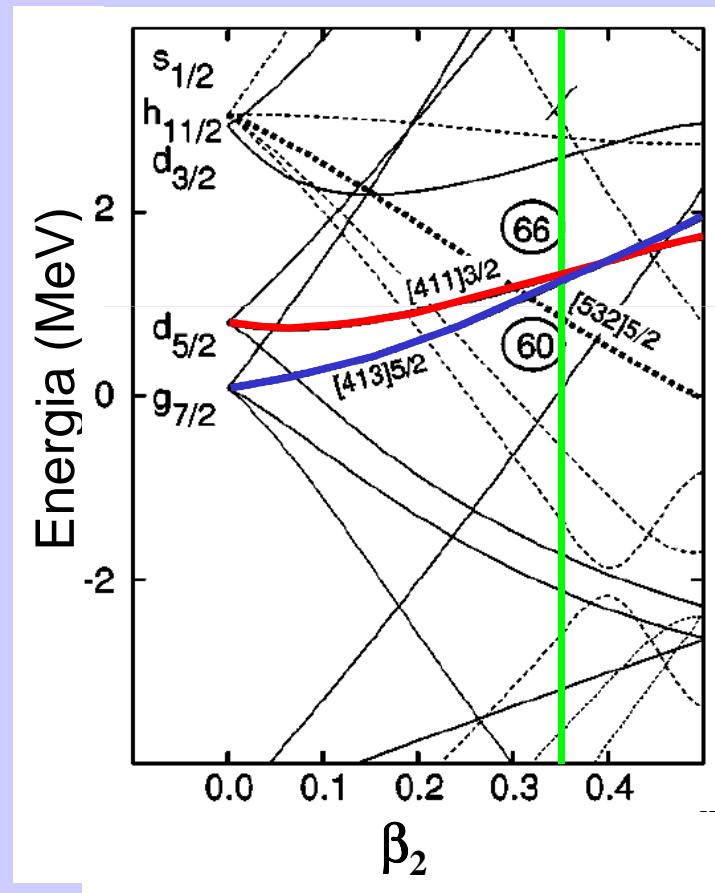
# Fine structure in the $p$ -decay of $^{131}_{63}\text{Eu}$



**Systematics of  $E(2^+)$  vs  $\beta_2$**   
 $E(2^+) = 121 \text{ keV} \Leftrightarrow \beta_2 \approx 0.35$

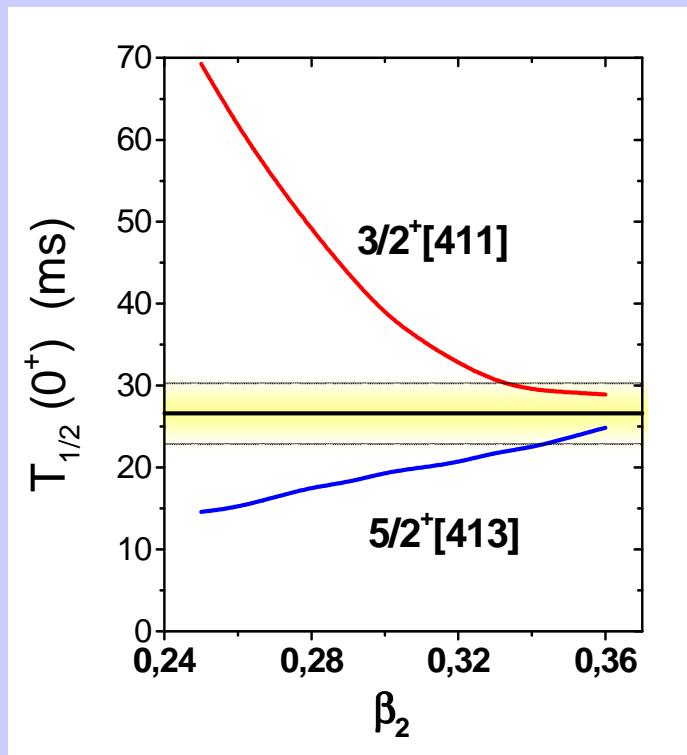
# WF structure of odd proton in $^{131}_{63}\text{Eu}$

$$\Omega^\pi[N, n_z, \Lambda] = \sum_{l,j} c_{lj} |N, \ell, j\rangle$$

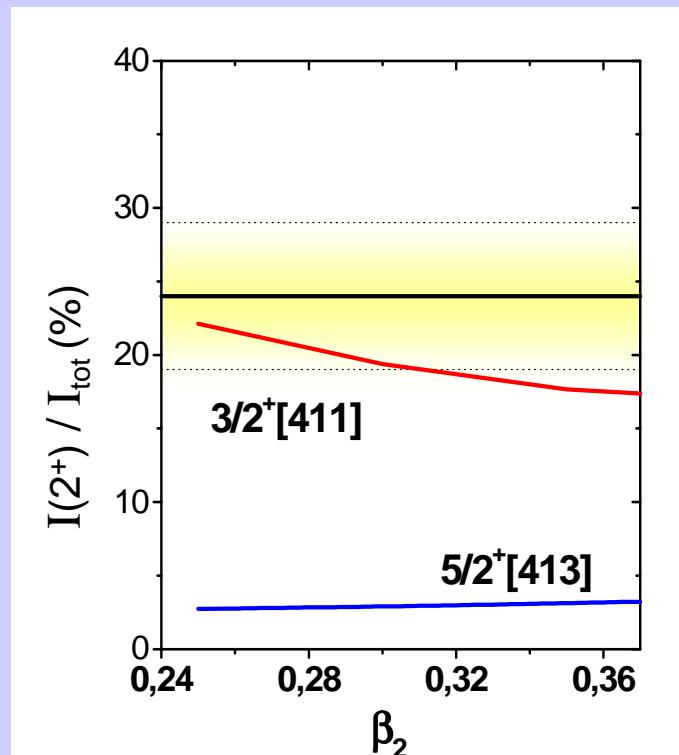


# Calculations including deformation

## Lifetime



## feeding of $2^+$



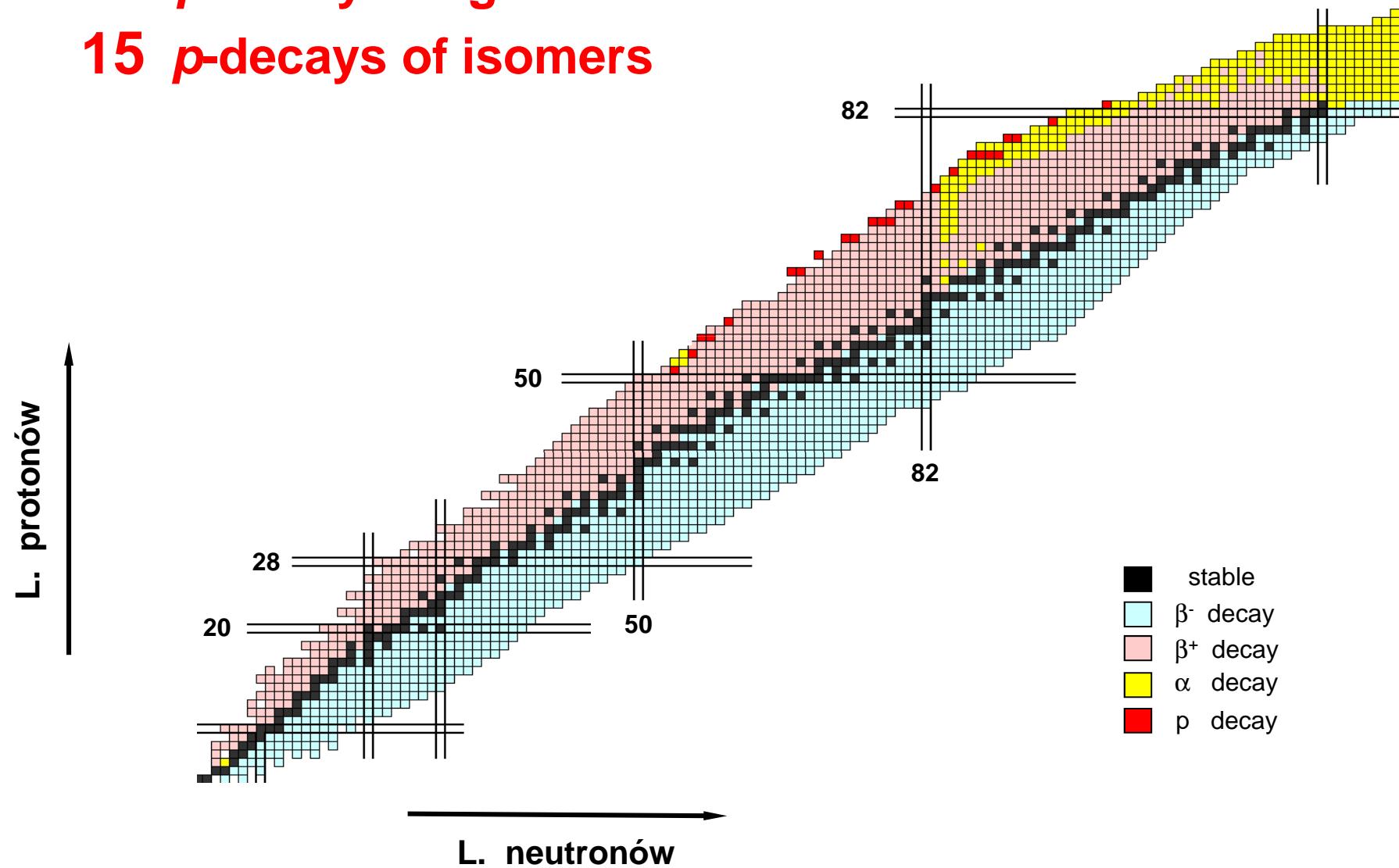
**Conclusion:**

proton emission from deformed  $3/2^+[411]$  state observed

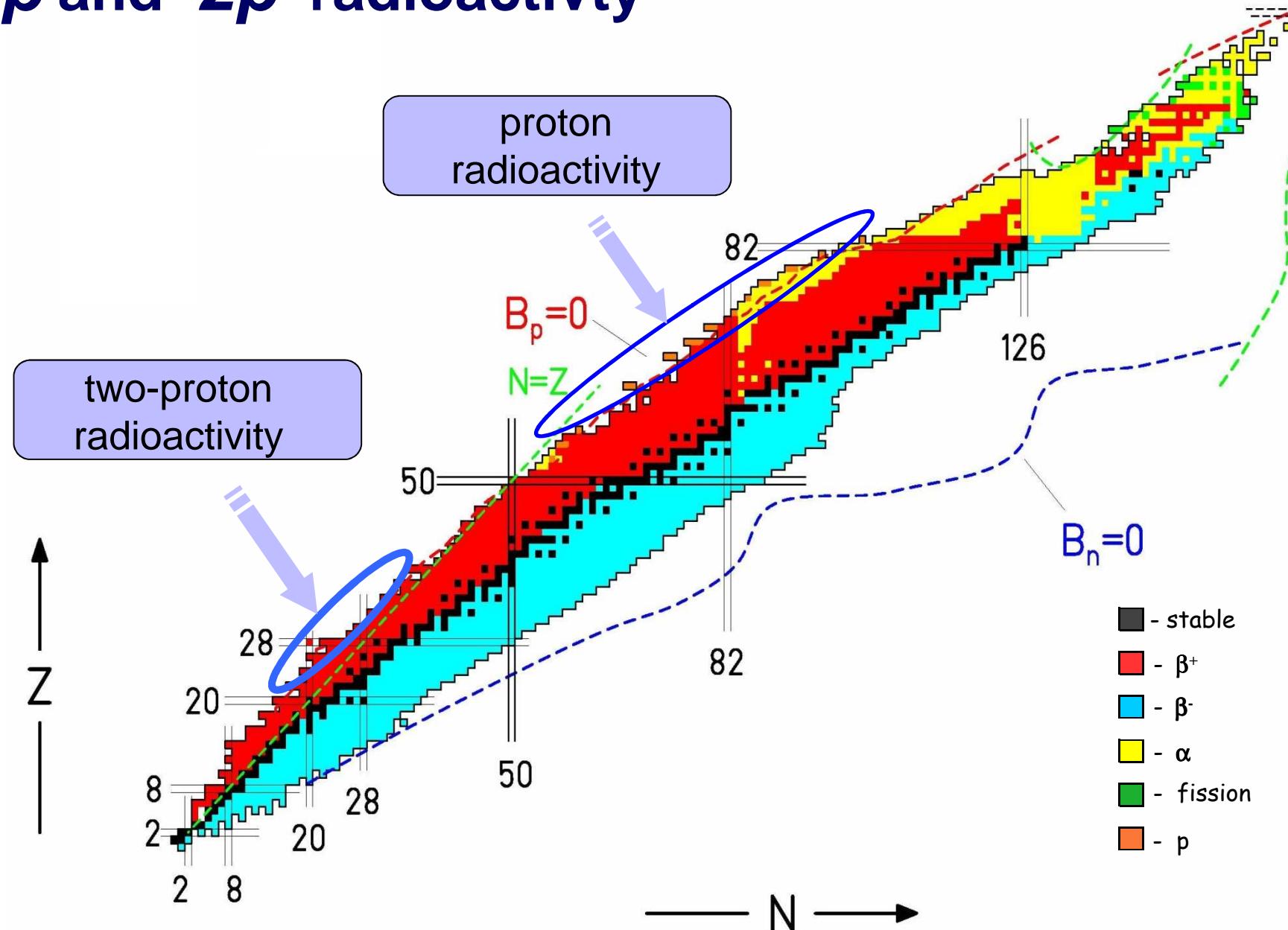
# Known proton emitters

30 *p*-decays of ground states

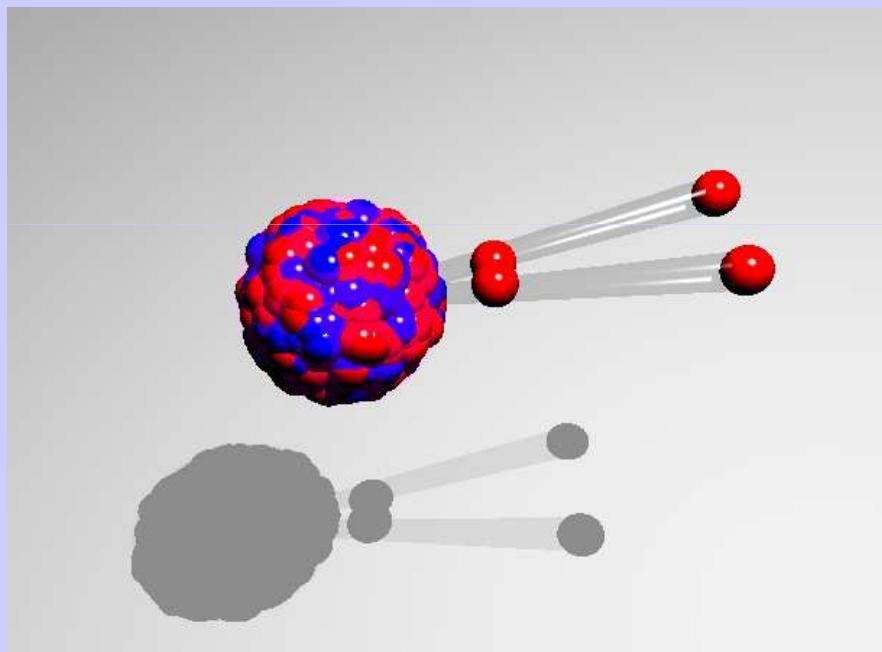
15 *p*-decays of isomers



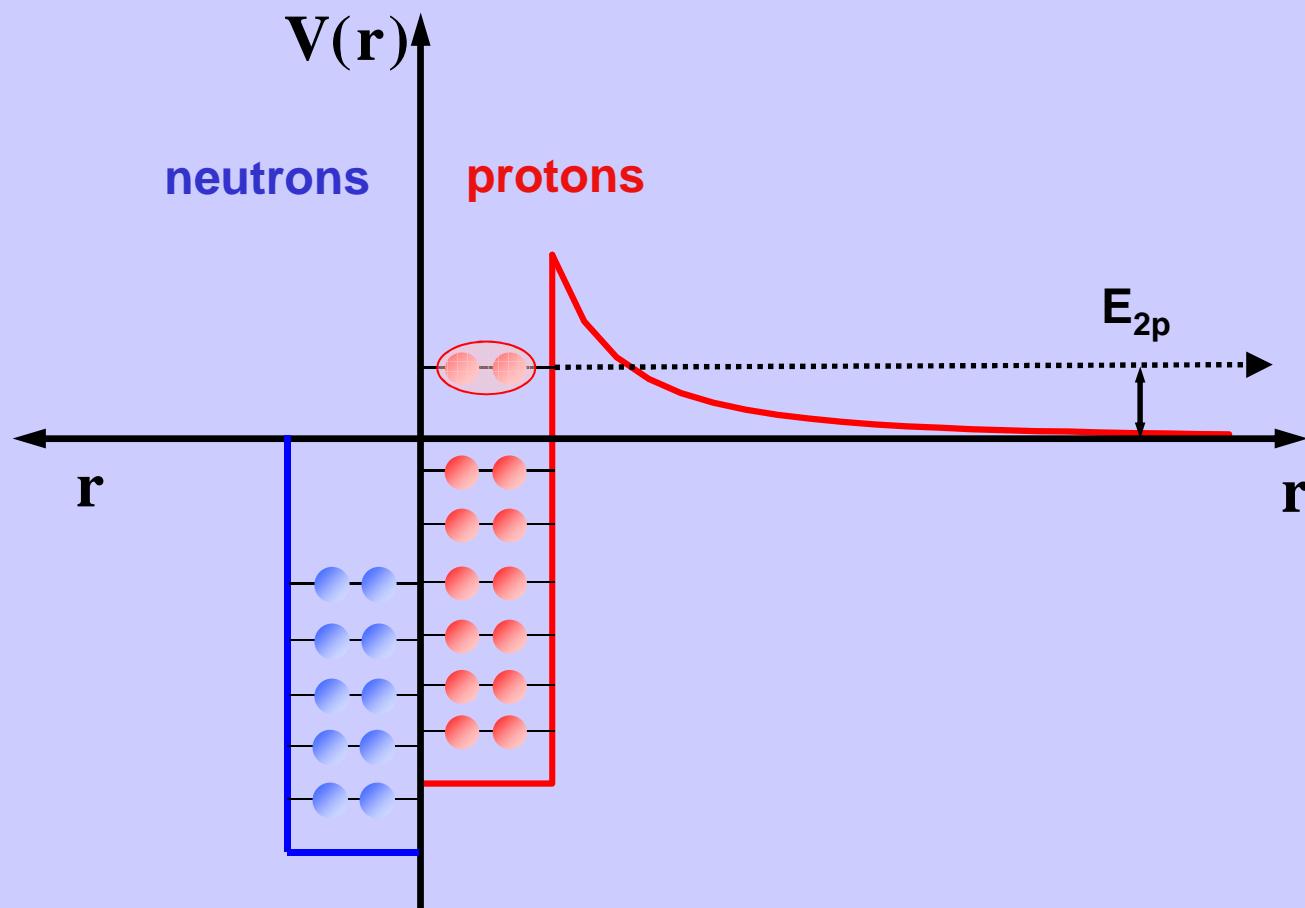
# *p* and *2p* radioactivity



## Two-proton radioactivity (3 isotopes)

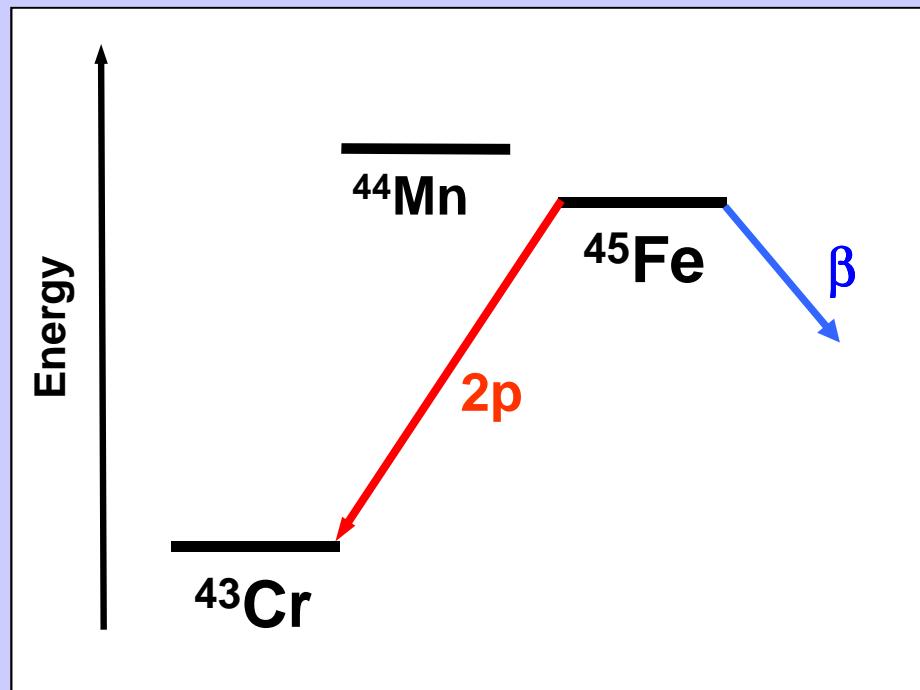
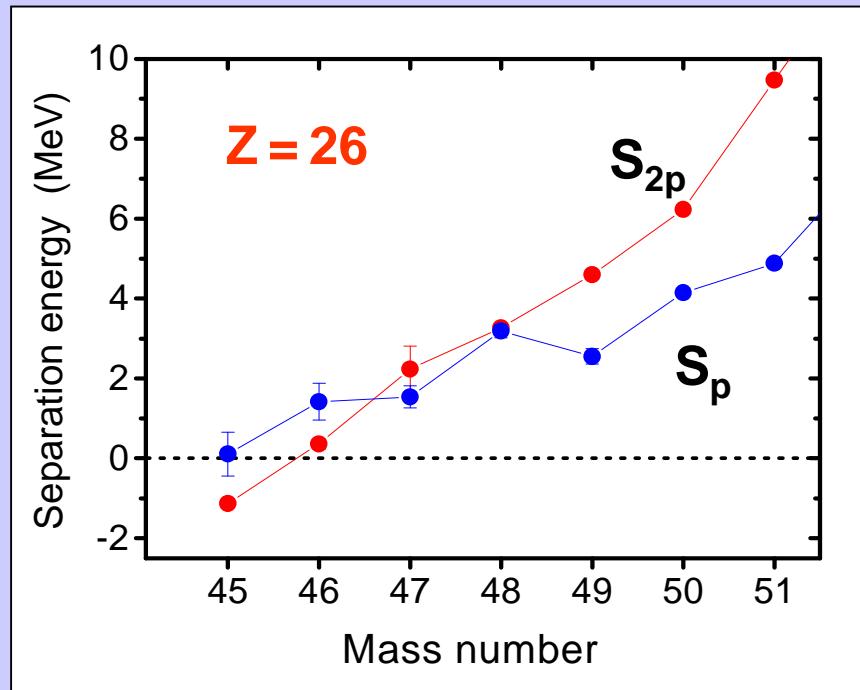


# $2p$ emission process



# Two-proton radioactivity

- prediction - V. Goldansky in 1960

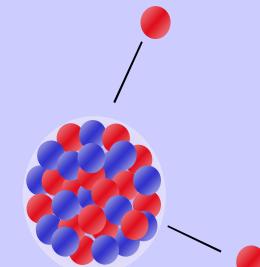
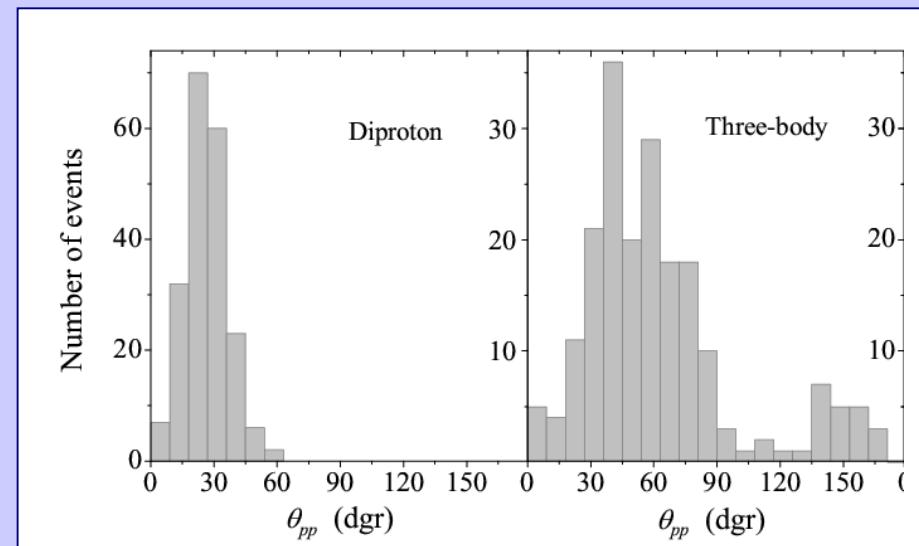
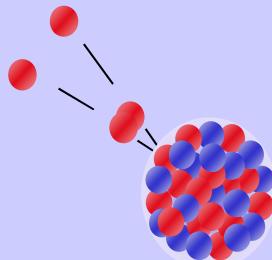


- single proton branch closed
- large  $Q_\beta$  value

# Experimental challenges

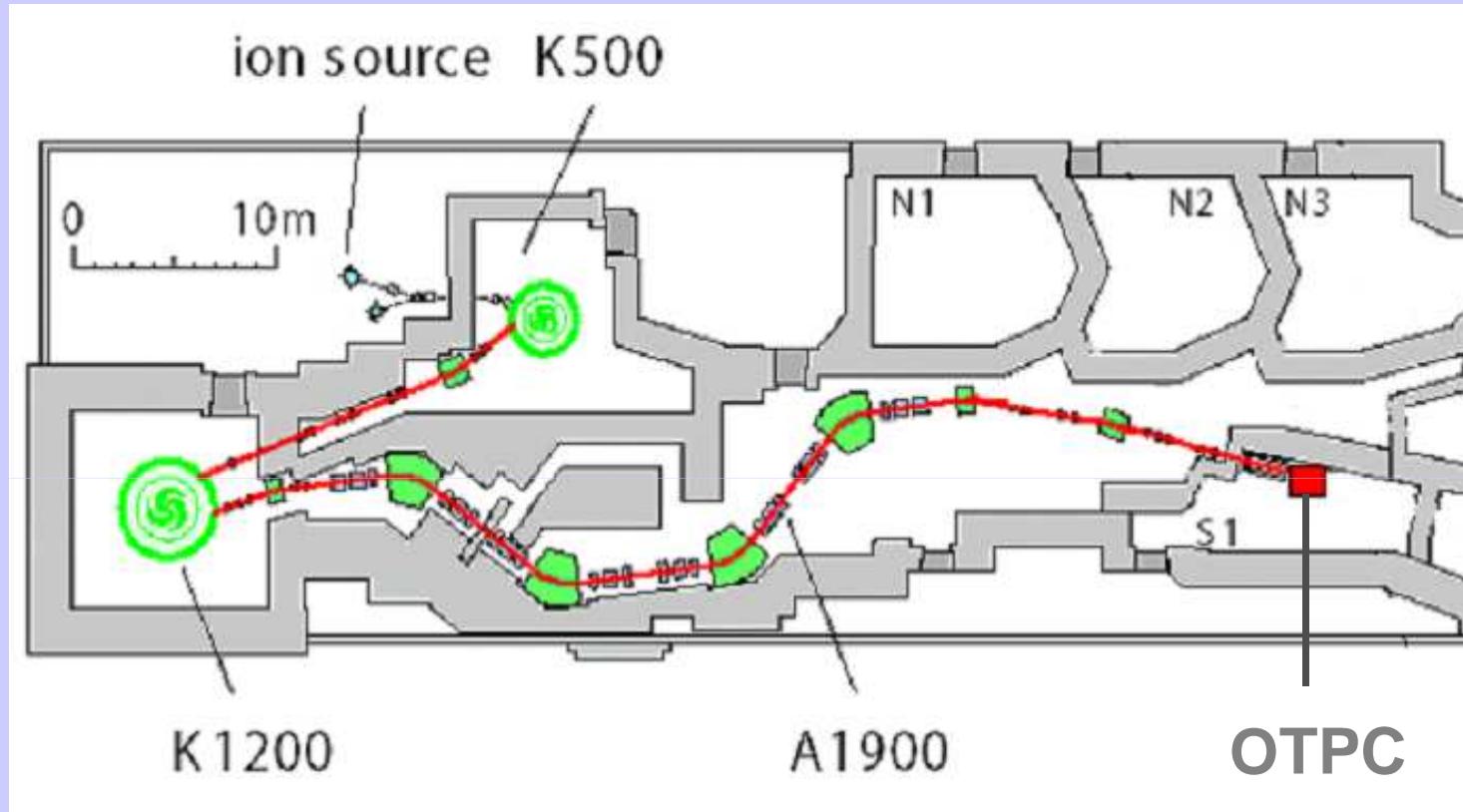
- detection of individual protons
- energy measurement
- determination of angular correlation

## Predicted $p$ - $p$ opening angle for $^{45}\text{Fe}$



L. Grigorenko : simulation for 200 events

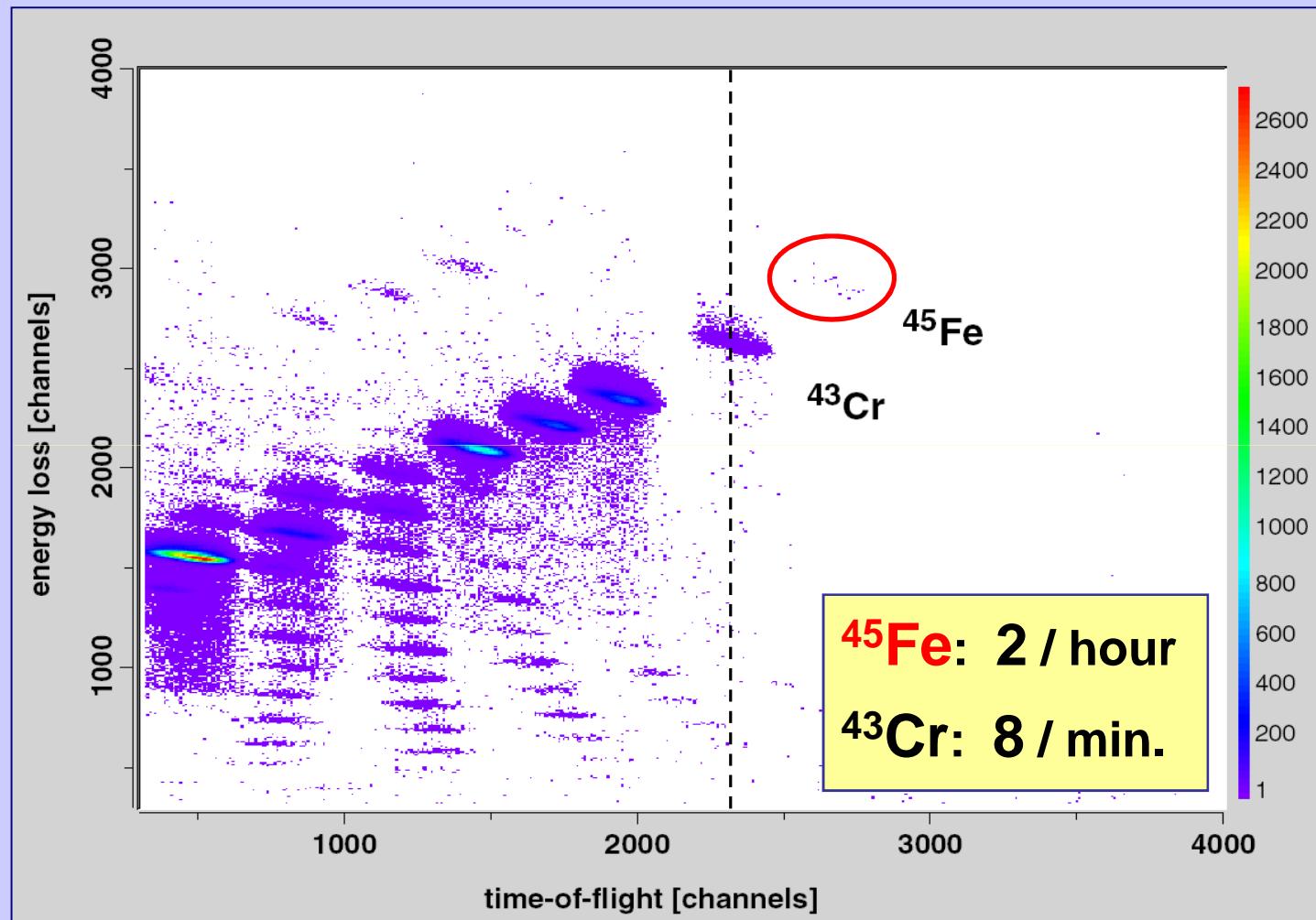
# Experiment at NSCL/MSU



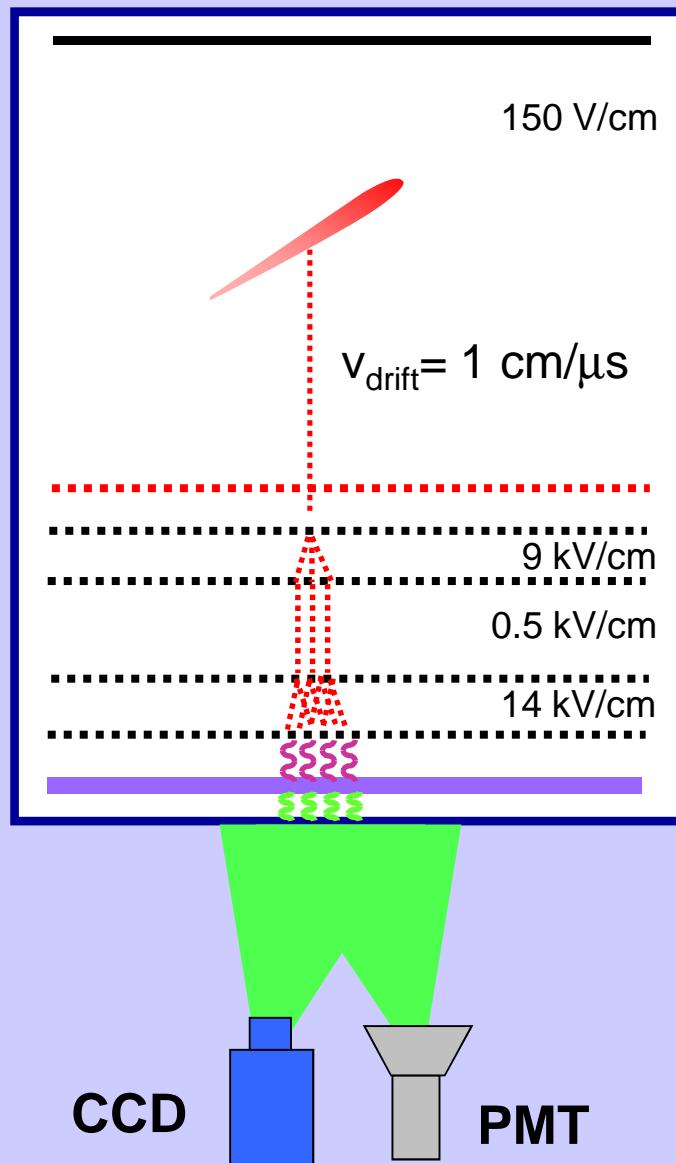
Production:  $^{58}\text{Ni}$  (161 MeV/u) +  $^{\text{nat}}\text{Ni}$   $\rightarrow$   $^{45}\text{Fe}$

Identification in-flight:  $\Delta E + \text{TOF}$

# Ion identification



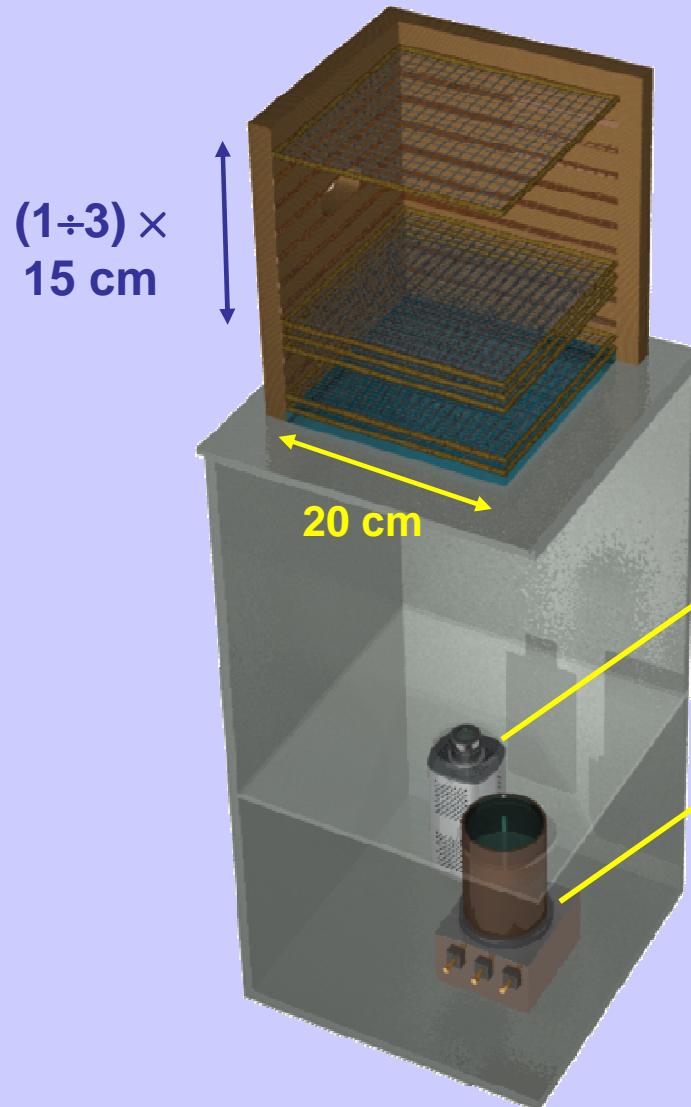
# Optical Time Projection Chamber



- active volume**  
66%He + 32%Ar
- gating electrode**
- amplification**
- light detection**

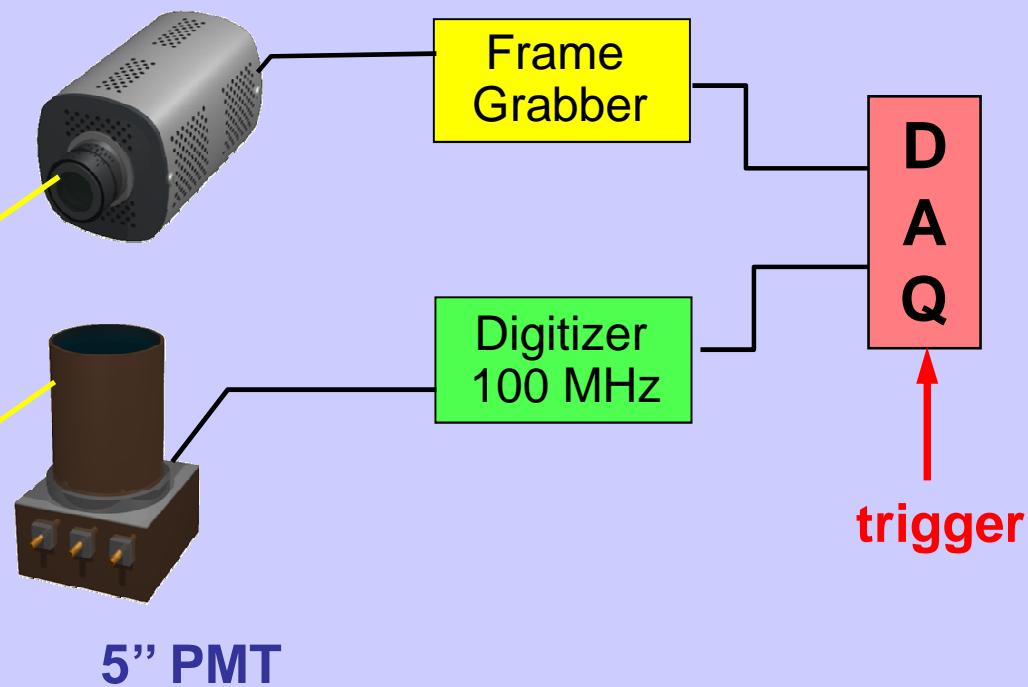
M. Ćwiok et al., IEEE TNS, 52 (2005) 2895  
K. Miernik et al., NIM A581 (2007) 194

# Optical Time Projection Chamber

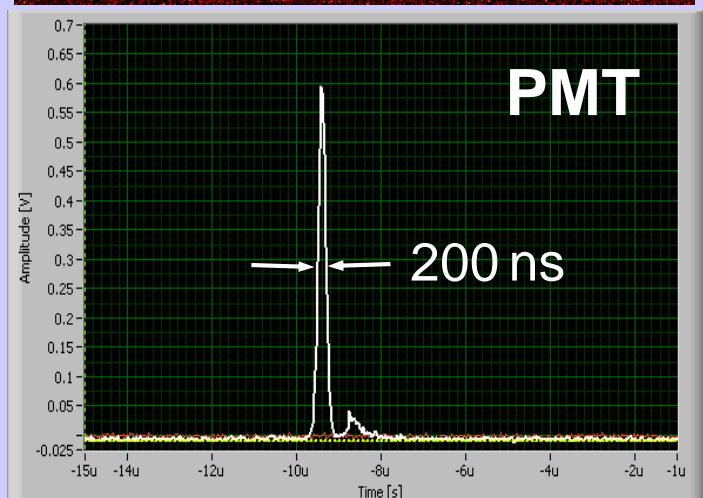
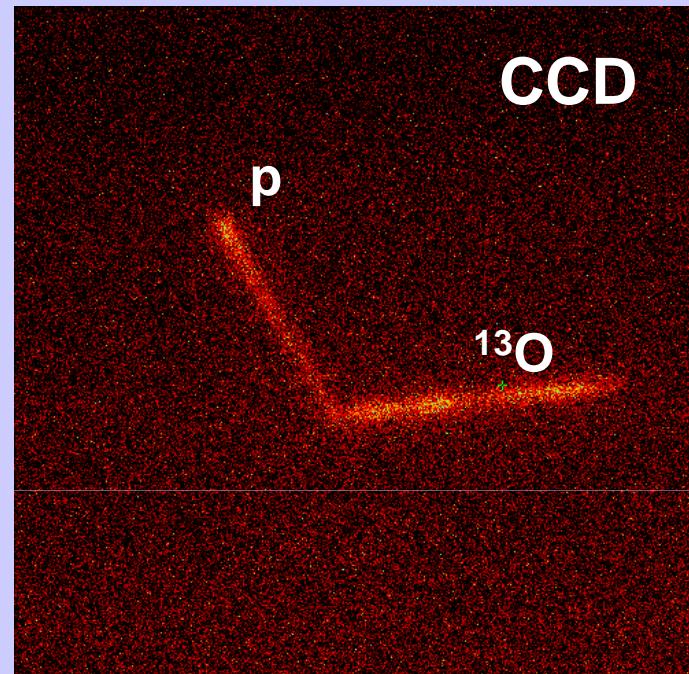
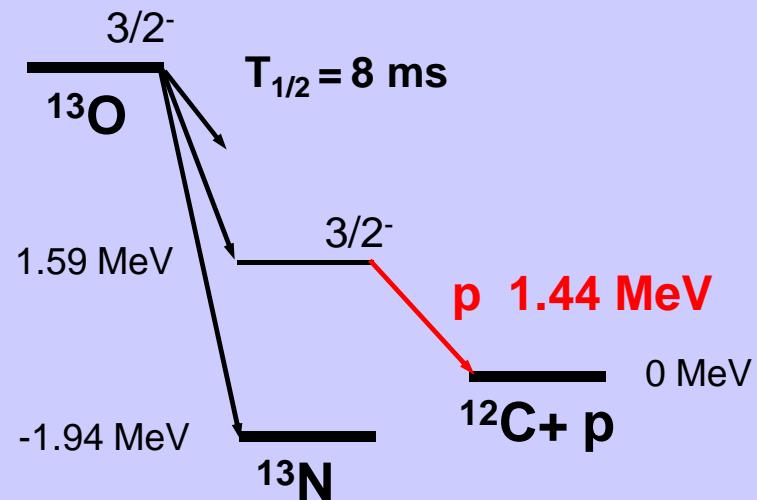


**CCD 2/3"**

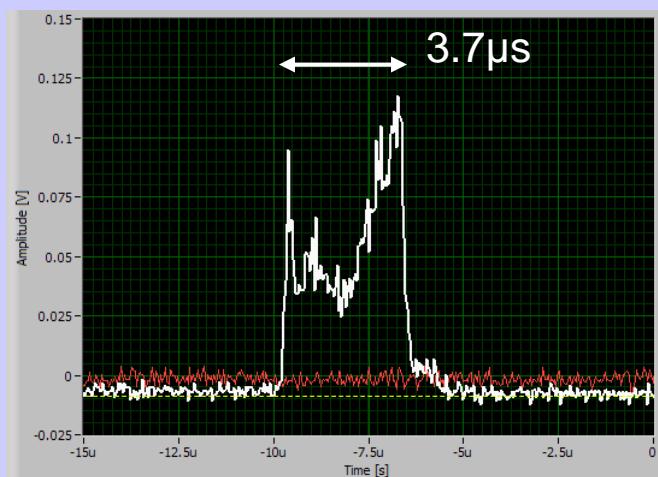
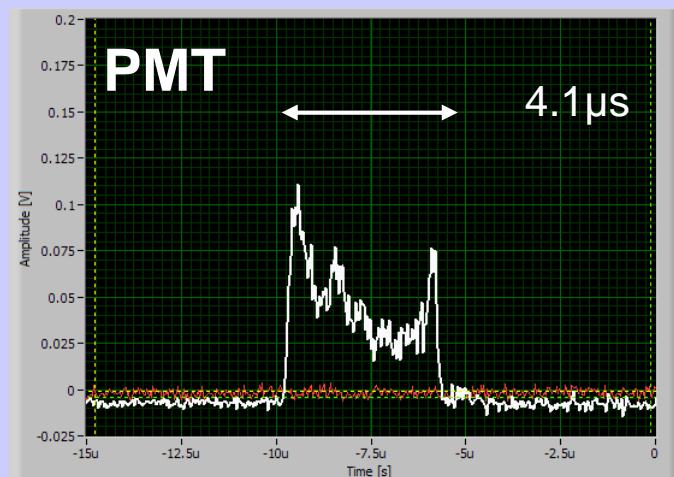
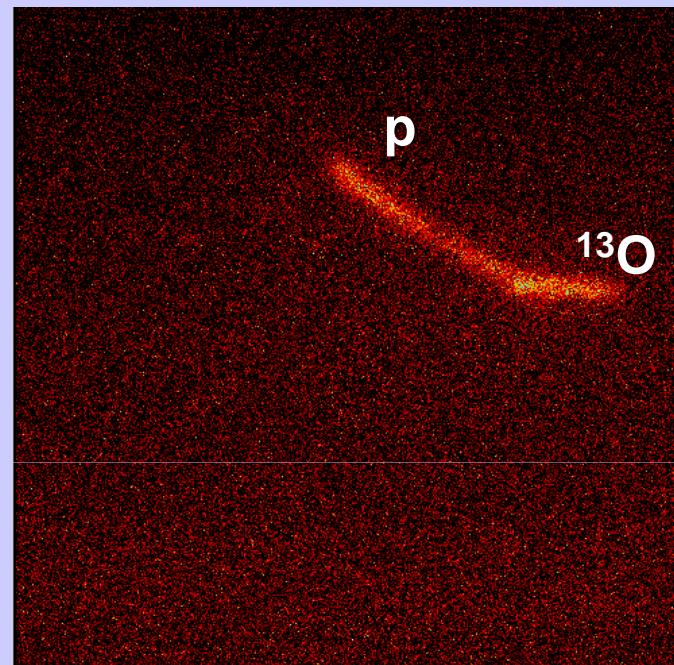
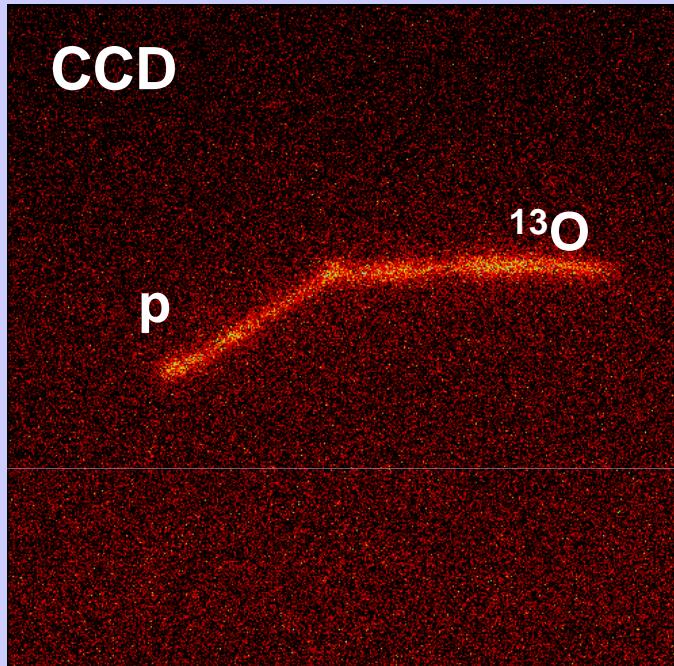
- $1000 \times 1000$  pix.
- 12-bits
- image ampl. ( $\times 2000$ )



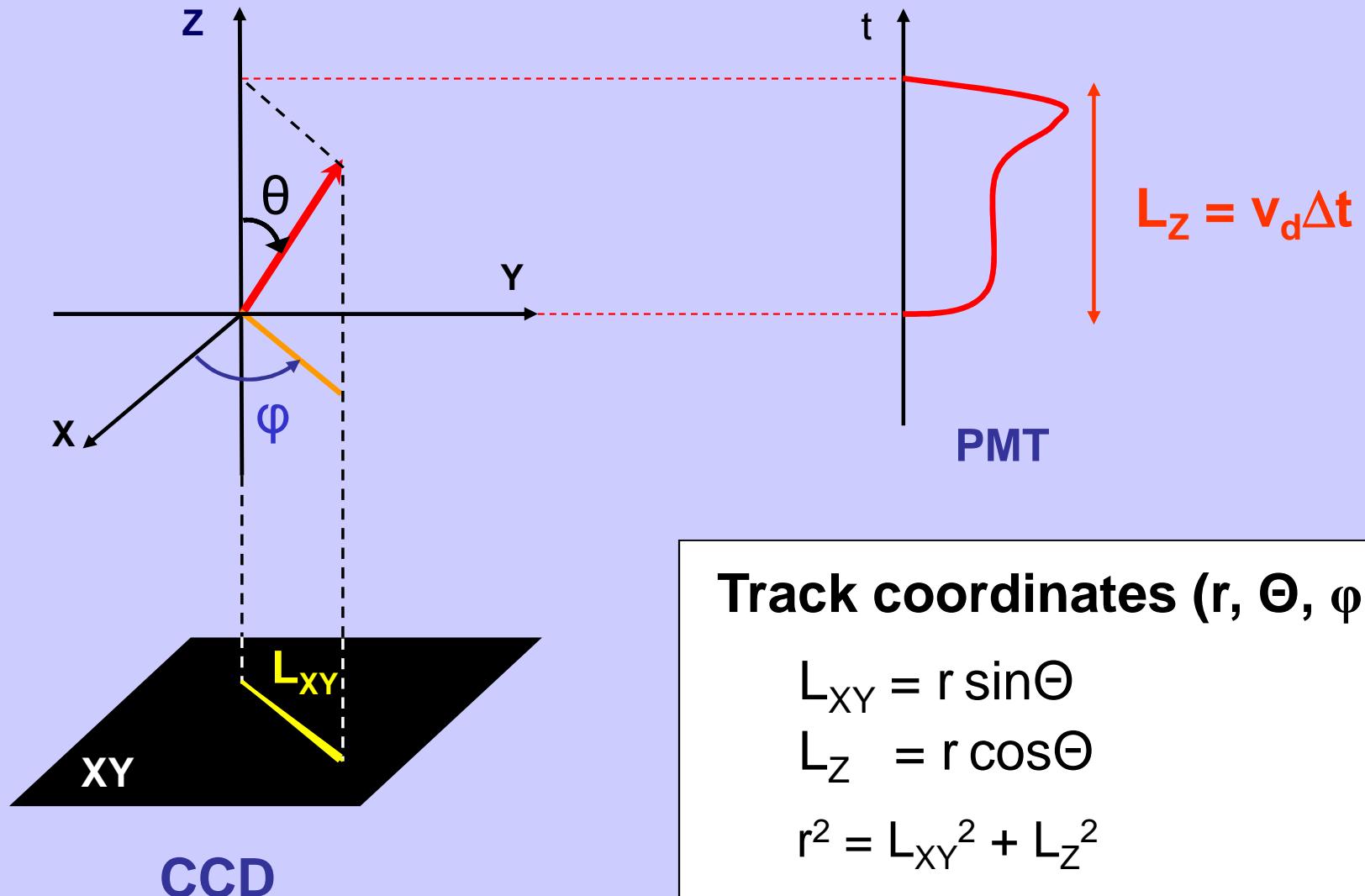
# Protons after beta decay of $^{13}\text{O}$



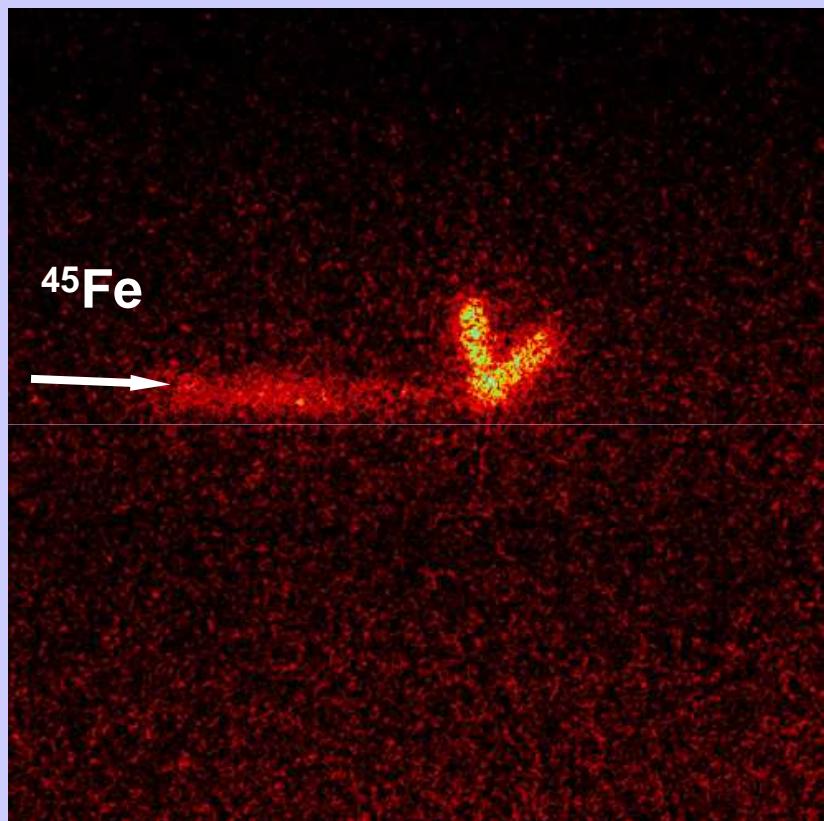
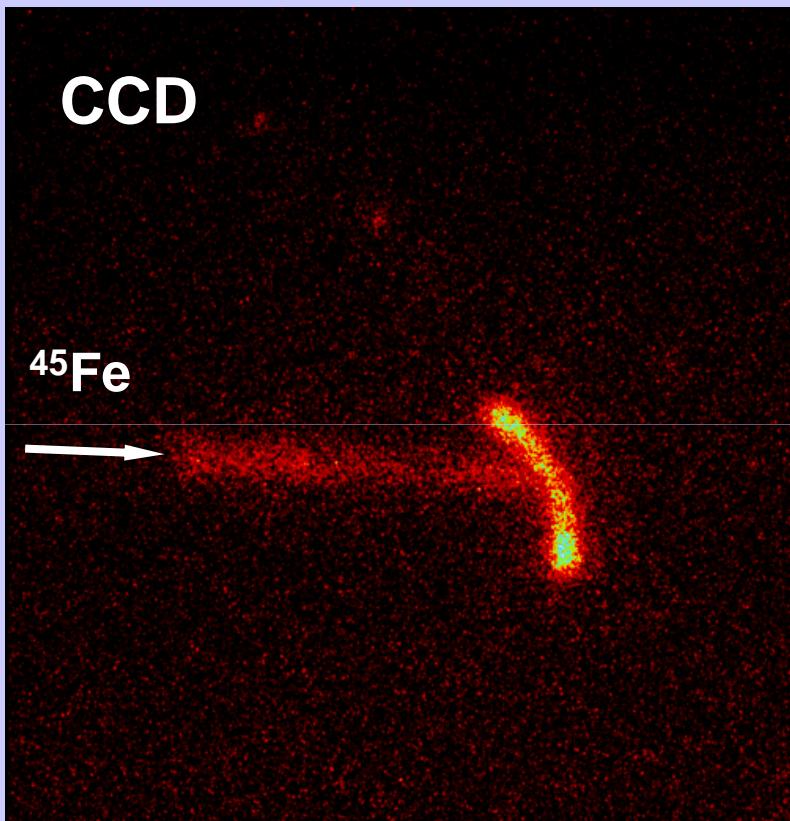
# Protons after beta decay of $^{13}\text{O}$



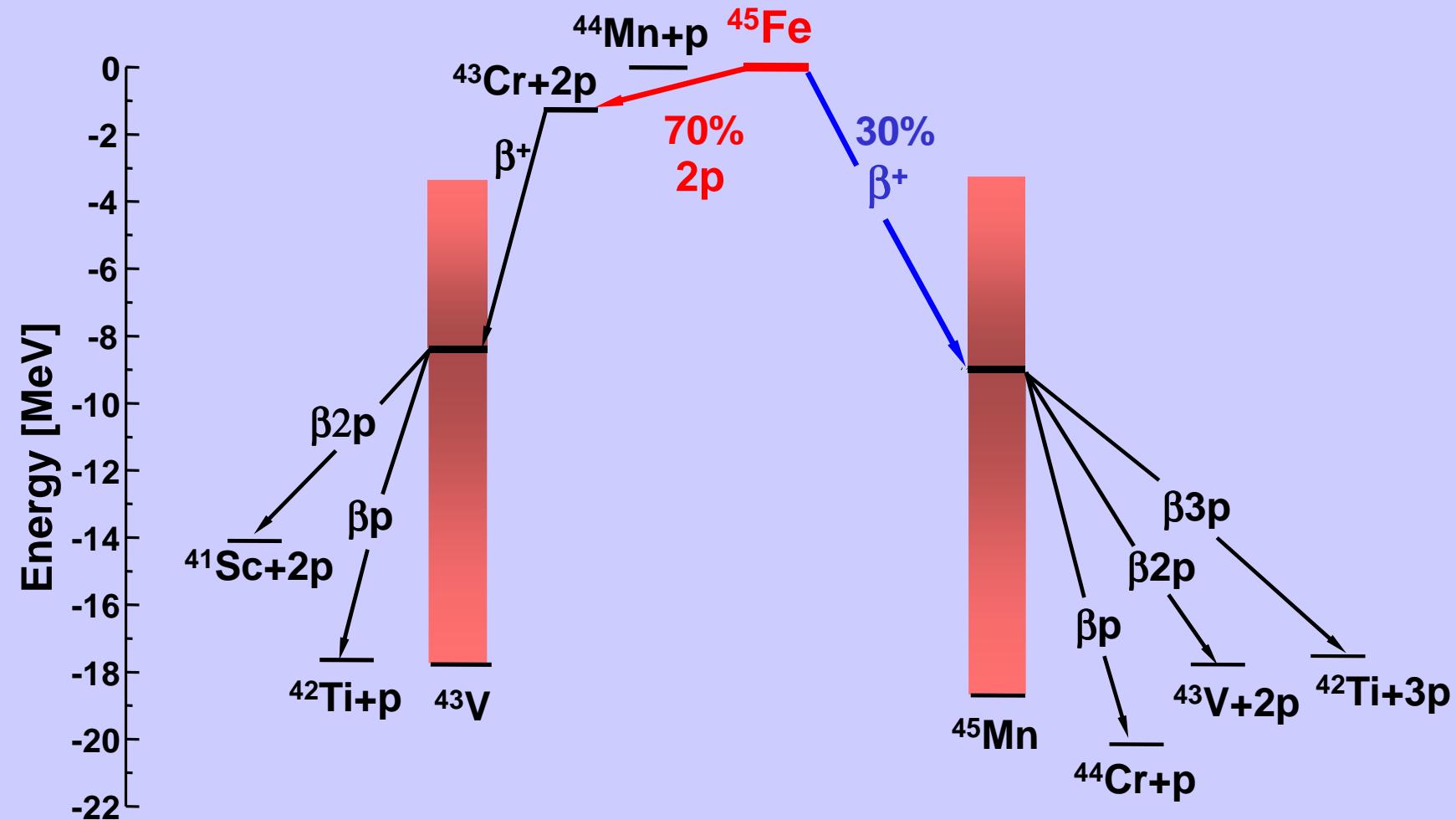
# Events reconstruction



# $2p$ decay of $^{45}\text{Fe}$

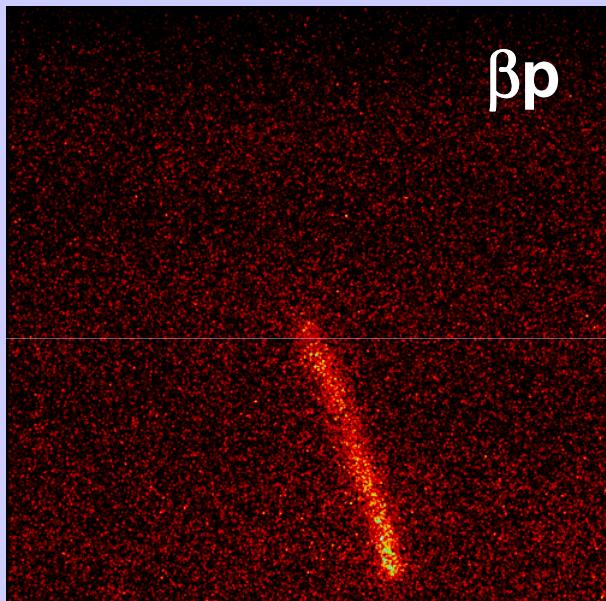


# Decay scheme of $^{45}\text{Fe}$

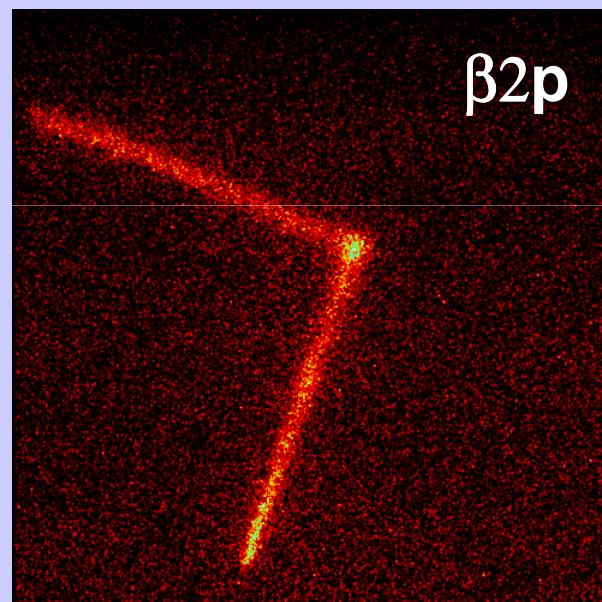


# $\beta^+$ decay of $^{45}\text{Fe}$

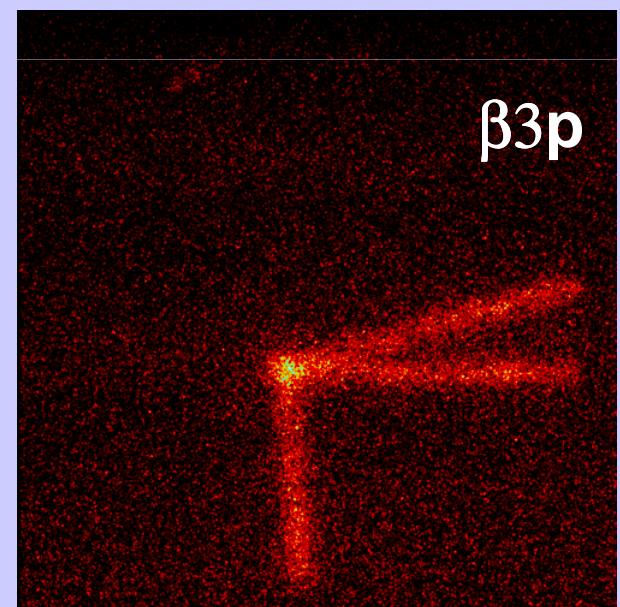
24 events



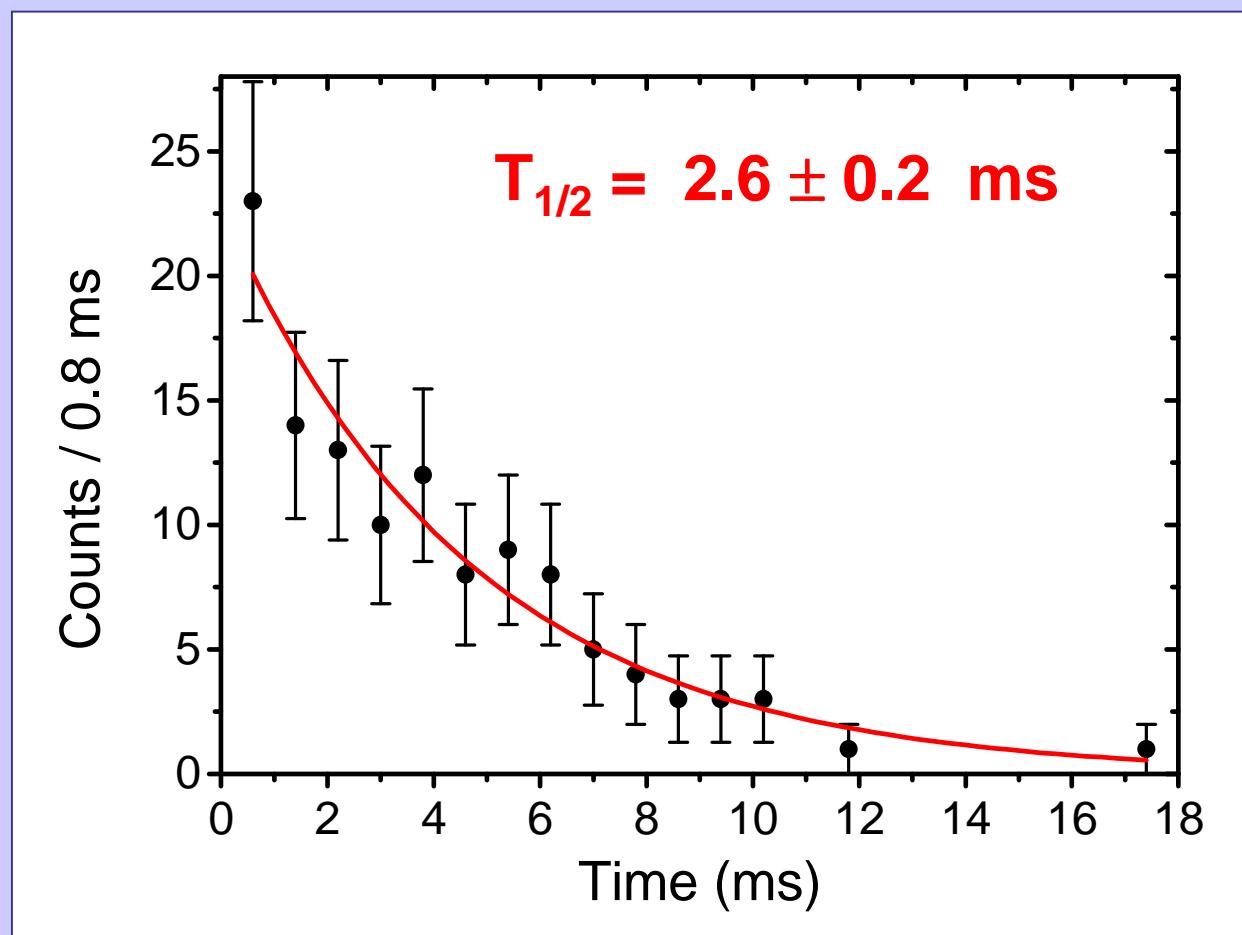
10 events



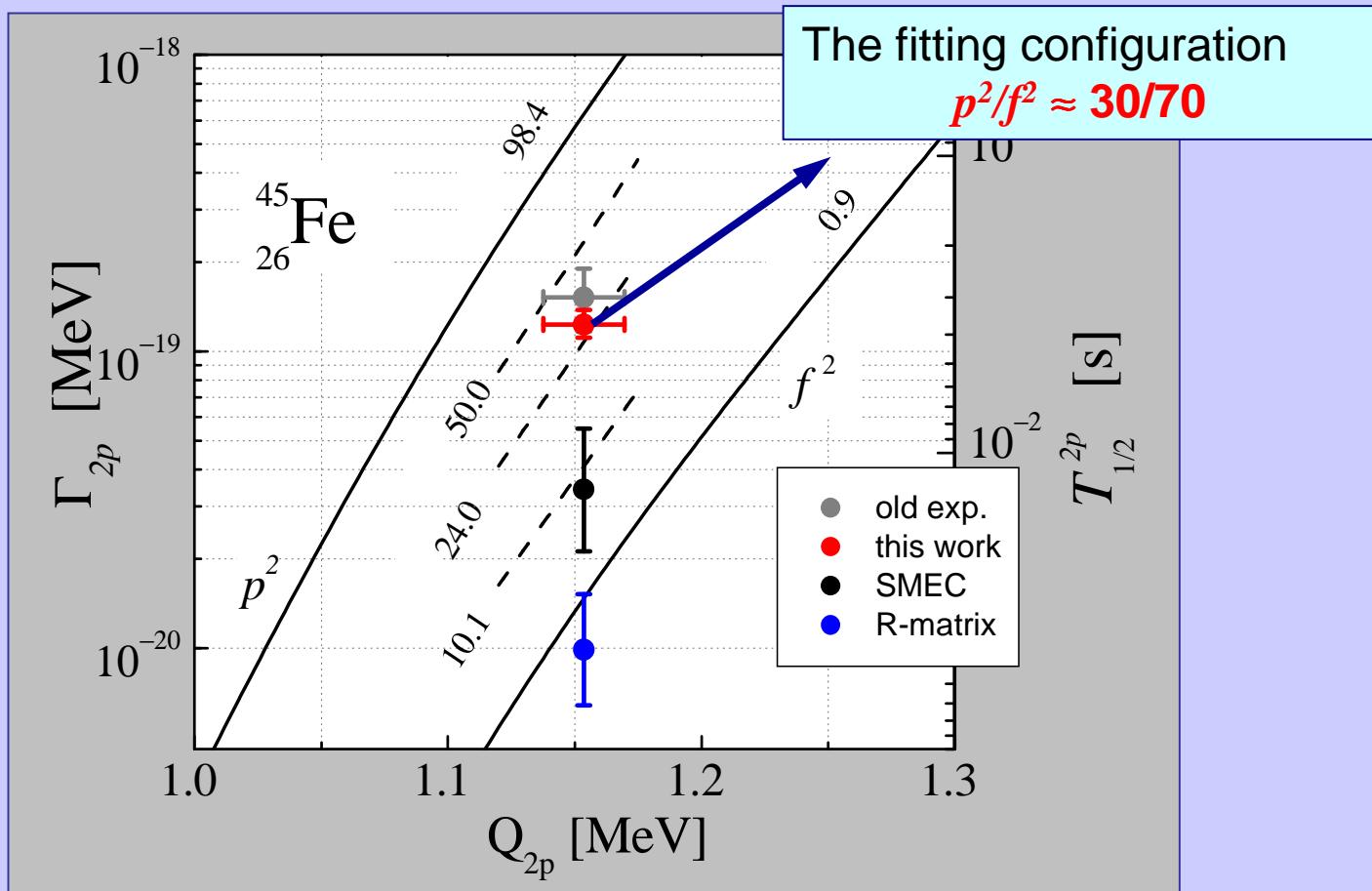
4 events



# Lifetime of $^{45}\text{Fe}$



# Partial $2p$ half-life of $^{45}\text{Fe}$

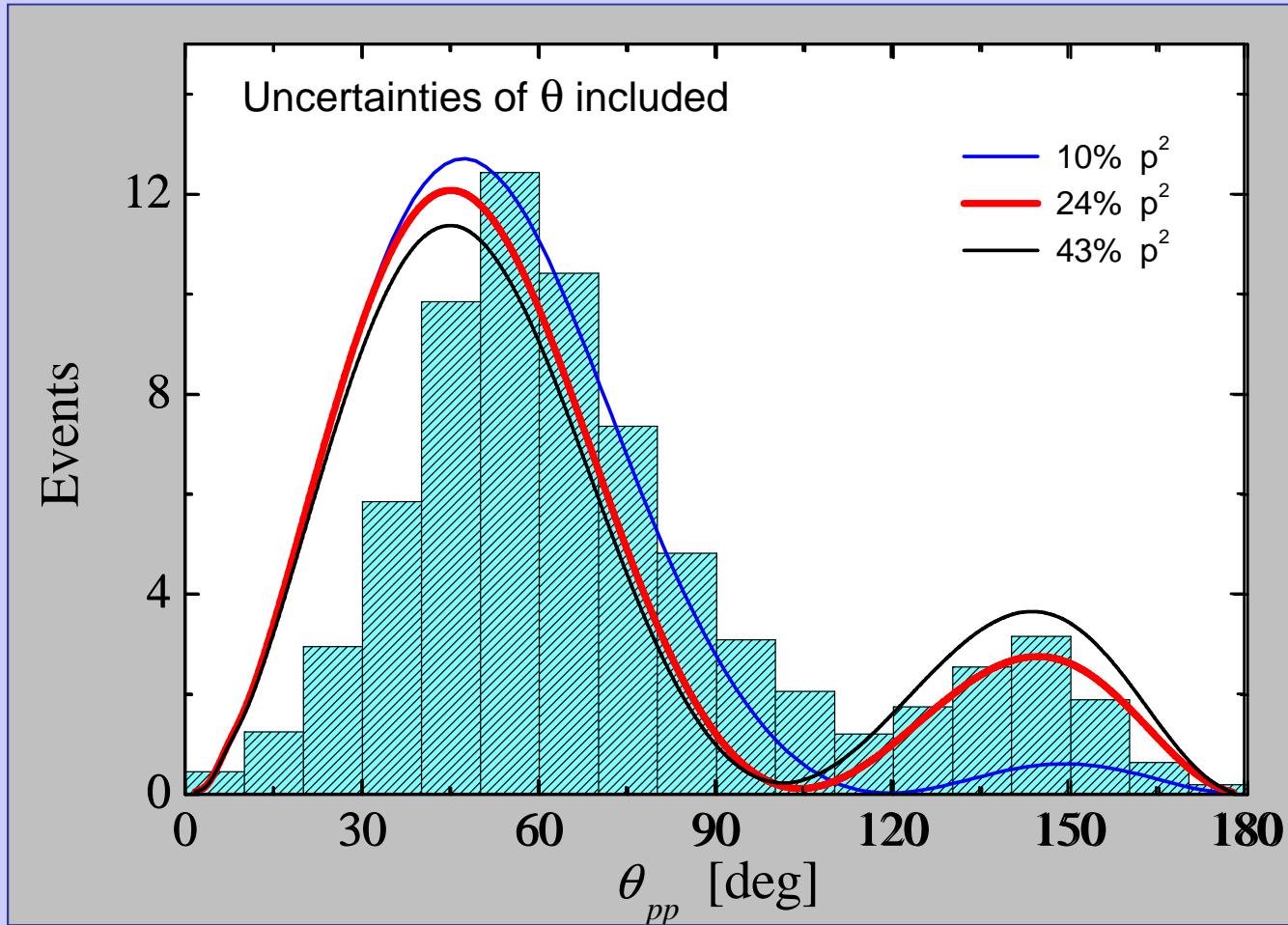


**3-body model:** L.V. Grigorenko and M.V. Zhukov, PRC 68 (2003) 054005

**SMEC:** J. Rotureau, J. Okołowicz, M. Płoszajczak, NPA 767 (2006) 13

**R-matrix:** B.A. Brown, F.C. Barker, PRC 67 (2003) 041304

# $p$ - $p$ angular correlation



K. Miernik *et al.*, PRL 99, 192501 (2007)

L.V. Grigorenko and M.V. Zhukov, PRC 68 (2003) 054005

# Summary

- **studies of  $p$  and  $2p$  decays provide information on:**
  - limits of nuclear existence
  - masses of exotic nuclei
  - sequence of single-particle states
  - structure of WF of nuclear states